

# Dynamical Polar Warming Amplification and a New Climate Feedback Framework

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**Cai (2005, 2006), Cai and Lu (2007): DPWA Theory**

**Lu and Cai (2009), Cai and Lu (2009): CFRAM**

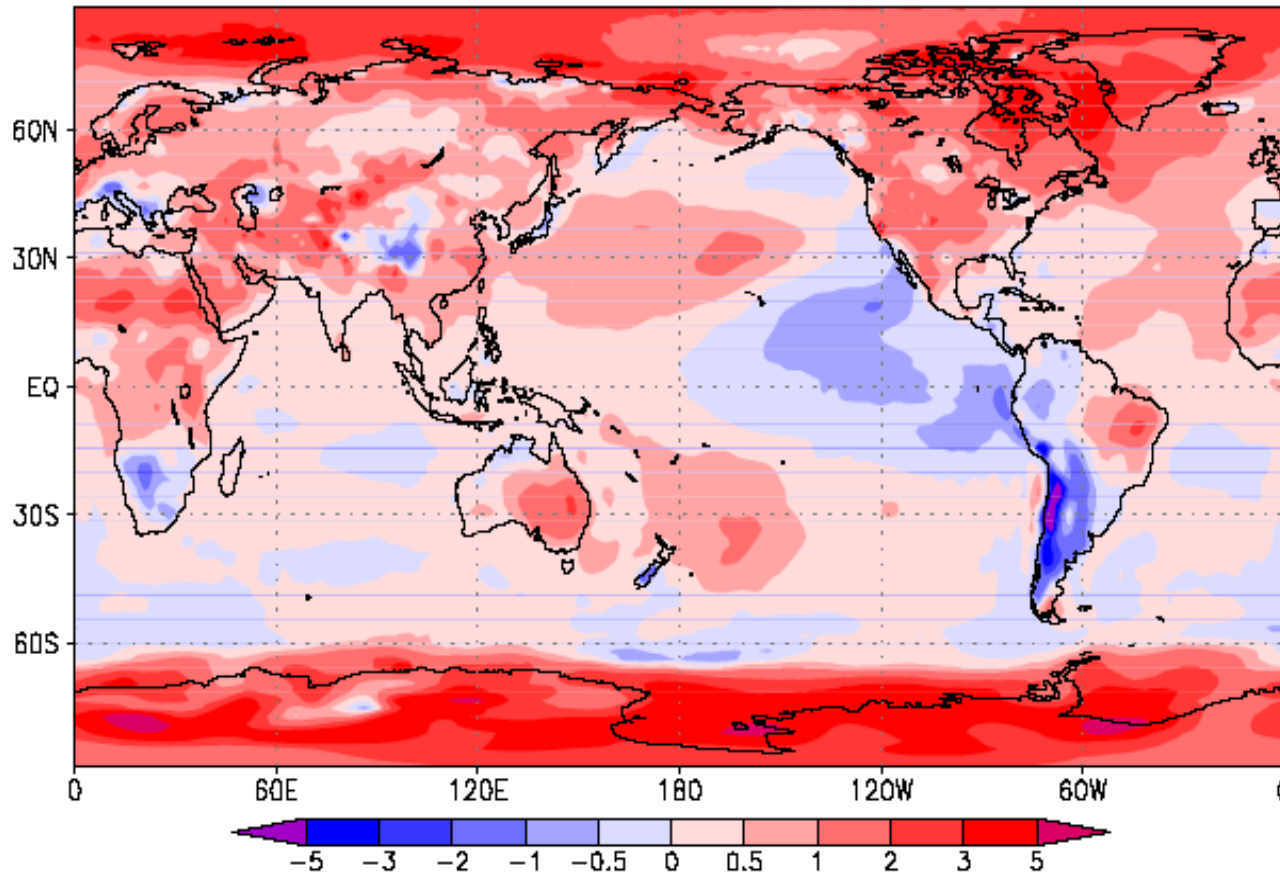
**Lu and Cai (2010) Cai and Tung (2013): Dynamical  
PWA in “dry” GCM**

**Taylor et al. (2013): all factors to PWA in NCAR CCSM4**

**Sergio et al. (2013): Seasonal cycle of PWA in CCSM4**

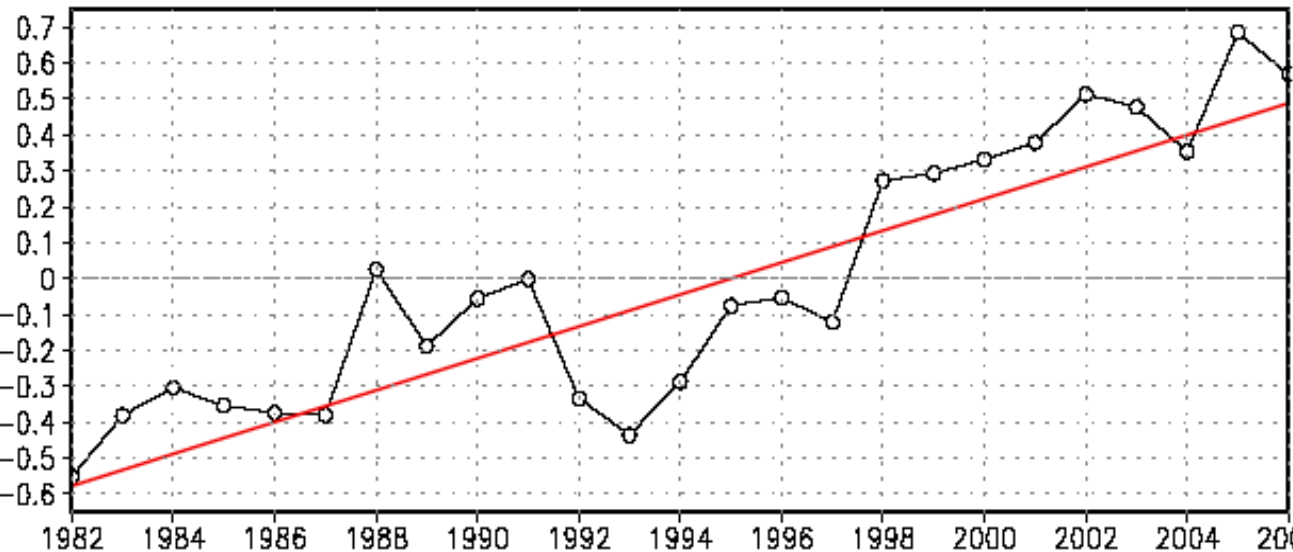
# Observed global warming pattern (NCEP R2)

d) EOF1 (30.21%)



**1st EOF  
(30% var.)**

b) PC1



**0.22 K/decade**

# Question 1

Is it POSSIBLE that a **stronger surface warming in high latitudes** than **low latitudes** in response to anthropogenic greenhouse gases can be CAUSED by the atmospheric poleward heat transport in the ABSENCE of **(positive) ice-albedo feedback in high latitudes** and **(negative) evaporation feedback in low latitudes**?

This question might sound paradoxical, given the fact the atmospheric poleward heat transport itself is driven by the poleward decreasing temperature profile.

**Cai (2005, 2006) answered this question: Yes**

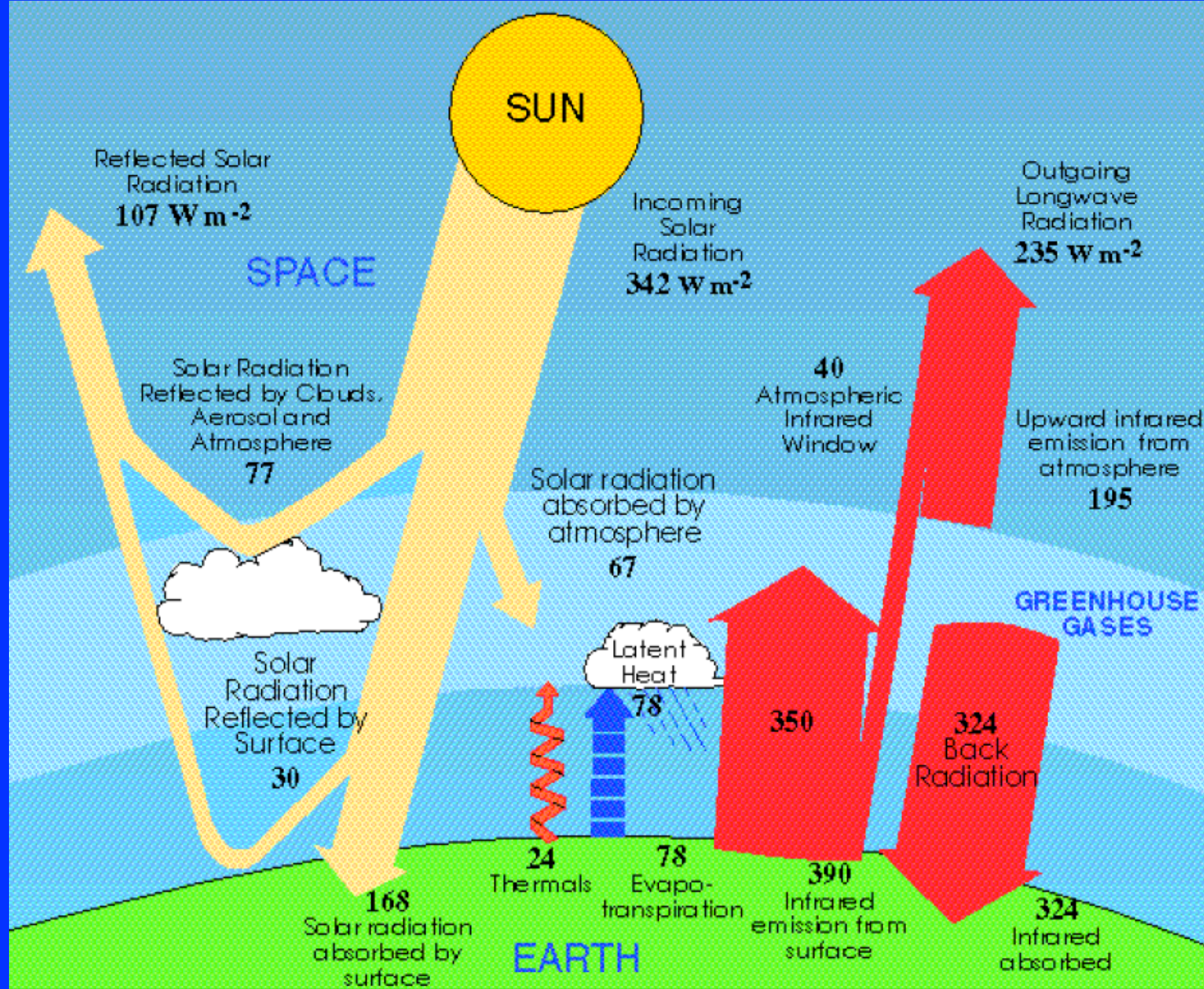
# Question 2

Can polar surface warming amplification by atmospheric dynamic feedback exist without polar warming amplification in the troposphere?

**Cai (2005, 2006) showed how and why an increase of air temperature gradient can still cause (i) a polar surface warming amplification (ii) a stronger surface warming than air warming in polar region.**



# Global mean atmosphere and surface energy balance: A single column perspective



# A dry radiative-transportive model

(Cai, 2005; 2006)

$D=0 \Rightarrow TOA=0$

$TOA > 0$

$TOA < 0$

$D=0 \Rightarrow TOA=0$

$\Delta \varepsilon > 0$  : "2CO<sub>2</sub> forcing"

$$D = \mu_A (A_1 - A_2)$$



$$\varepsilon \sigma G_1^4 - 2\varepsilon \sigma A_1^4 - D = 0$$

$$\varepsilon \sigma G_2^4 - 2\varepsilon \sigma A_2^4 + D = 0$$

$$S_1 - \sigma G_1^4 + \varepsilon \sigma A_1^4 = 0$$

$$S_2 - \sigma G_2^4 + \varepsilon \sigma A_2^4 = 0$$

0° Low-lat. Boxes

30° High-lat. Boxes

90°

A: air temperature; G: surface temperature

j = 1: low latitudes; j = 2: high latitudes



# Analytic Solution of the 4-box dry model

- Change in atmospheric equator-to-pole temperature contrast:**

$$\Delta(A_1 - A_2) = \frac{\sigma A_{E1}^3 A_{E2}^3 + \mu_A \frac{A_{E1}^3 + A_{E2}^3}{\varepsilon^2}}{(4\sigma A_{E1}^3 A_{E2}^3 + \mu_A \frac{A_{E1}^3 + A_{E2}^3}{(2-\varepsilon)\varepsilon})} (A_{E1} - A_{E2}) \frac{\Delta\varepsilon}{(2-\varepsilon)} > 0$$

where  $A_{Ej}$  are the (“1CO2”) equilibrium air temperatures for  $\Delta\varepsilon = 0$ .

- Change in the surface equator-to-pole temperature contrast**

$$\Delta(G_1 - G_2) = \frac{G_{E1} - G_{E2}}{4} \frac{\Delta\varepsilon}{(2-\varepsilon)} - 2\mu_A \frac{\Delta(A_1 - A_2)}{4\sigma G_{Ej}^3 (2-\varepsilon)}$$

where  $G_{Ej}$  are the (“1CO2”) equilibrium surf. temperatures for  $\Delta\varepsilon = 0$ .

How is it possible that an increase of air temperature gradient can cause reduction of the surface temperature gradient?

# Partial temperature changes in the dry model

(A prototype model that leads to the CFRAM)

$$\Delta A_j = \frac{1}{4\sigma A_{Ej}^3} \left\{ \underbrace{\left( \sigma A_{Ej}^4 - \frac{(-1)^j D_{Ej}}{\varepsilon_{Ej}^2} \right)}_{(2 - \varepsilon_{Ej})} \frac{\Delta \varepsilon_{ext}}{(2 - \varepsilon_{Ej})} + \frac{(-1)^j \Delta D}{(2 - \varepsilon_{Ej}) \varepsilon_{Ej}} \right\}$$

$$\Delta G_j = \frac{1}{4\sigma G_{Ej}^3} \left\{ \underbrace{\sigma G_{Ej}^4}_{(2 - \varepsilon_{Ej})} \frac{\Delta \varepsilon_{ext}}{(2 - \varepsilon_{Ej})} + \frac{(-1)^j \Delta D}{2 - \varepsilon_{Ej}} \right\}$$

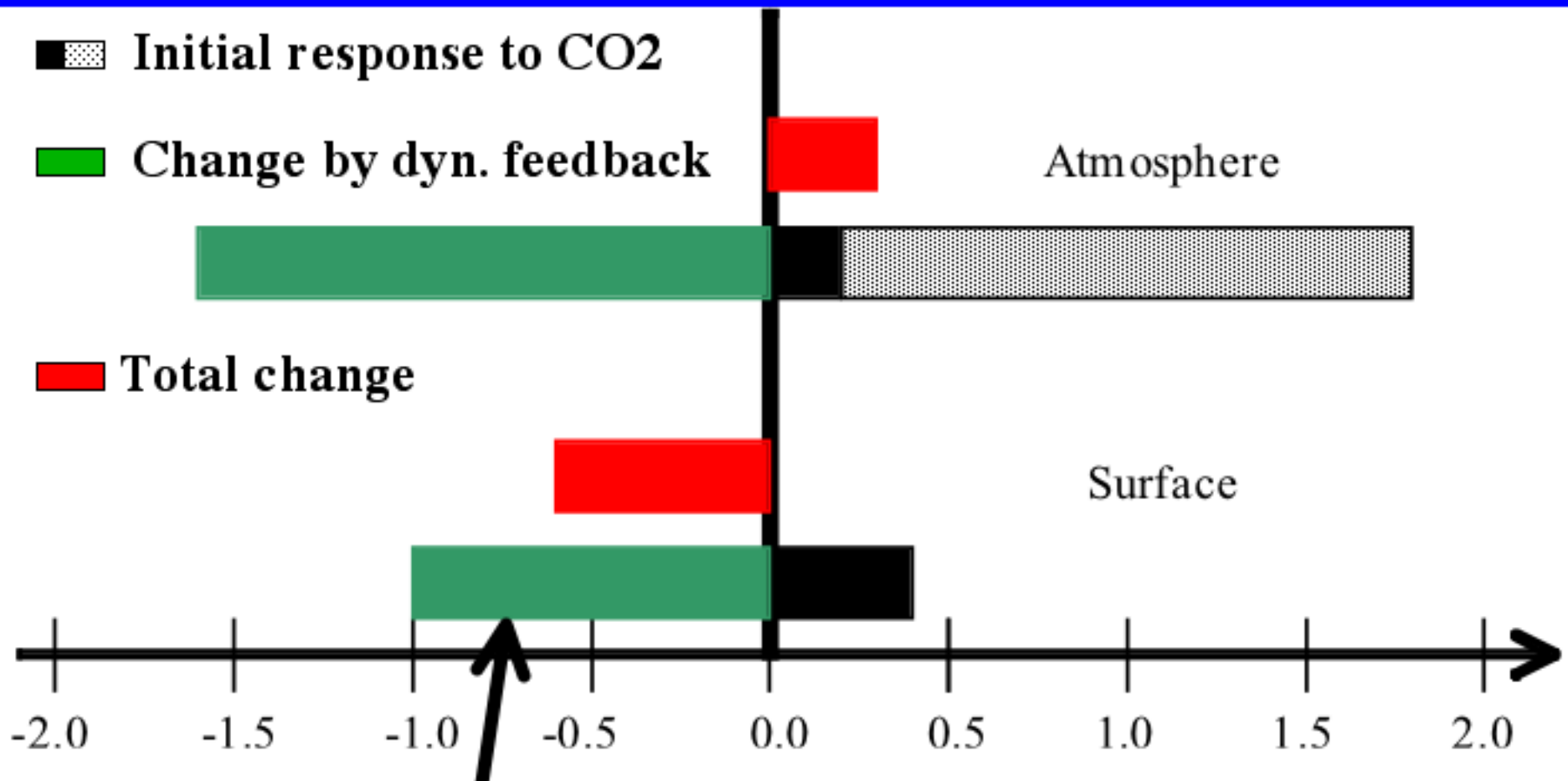
**j = 1: low latitudes**

**j = 2: high latitudes**

The additional SURFACE warming in high latitudes is due to the **more “BACK-RADIATION”** from a **warmer atmosphere in high latitudes** resulting from an increase in poleward heat transport ( $\Delta D > 0$ ) => **“greenhouse-plus” feedback in high latitudes.**

The reduction of SURFACE warming in low latitudes is due to the **less “BACK-RADIATION”** from a **colder atmosphere in low latitudes** resulting from  $\Delta D > 0$  => **“greenhouse-minus” feedback in low latitudes.**

# Change of meridional temperature gradient due to external forcing alone versus that due to dynamic feedback in the dry model



Due to Greenhouse-plus feedback in High Latitudes and Greenhouse-minus feedback in Low Latitudes

7

Figure 9 in Cai (2006)

# A brief overview of the Partial Radiative Perturbation (PRP) method

(designed for a globally uniform  
**SURFACE** warming)

# General definition of feedback

- **Forcing: an energy input to the system**
- **Response: an output of the system**
- **A feedback: an “induced input from the output”**
  - **Positive feedback: enhance the original energy input.**
  - **Negative feedback: reduce/oppose the original energy input.**



# Partial Radiative Perturbation Method

- **Forcing:** a radiative flux perturbation at the TOA
- **Response:** surface temperature (or system temperature)
- **Feedback:** additional radiative flux perturbations at the TOA in response to surface temperature

$$\Delta F^{TOA} = -(\Delta S_{TOA} - \Delta OLR_{TOA}) = -\frac{d(S_{TOA} - OLR_{TOA})}{dT_S} \Delta T_S$$

$$\lambda_{tot} = \frac{d(S_{TOA} - OLR_{TOA})}{dT_S}$$

$$\Delta T_S = \frac{F^{TOA}}{-\lambda_{tot}} = G_{tot} F^{TOA}$$

$\lambda_{tot} < 0$ : (Total) Feedback parameter

The warmer surface temperature is, the more energy outputs from the climate system

$G_{tot} = (-\lambda_{tot})^{-1}$ : (Total) Gain of the climate system

# Partial Radiative Perturbation Method

$$\begin{aligned}
 \frac{d(S_{TOA} - R_{TOA})}{dT_S} &= \lambda_{tot} = -\frac{\partial R_{TOA}}{\partial T_S} + \frac{\partial(S_{TOA} - R_{TOA})}{\partial H_2O} \frac{d(H_2O)}{dT_S} + \frac{\partial(S_{TOA} - R_{TOA})}{\partial \alpha} \frac{d\alpha}{dT_S} \\
 &+ \frac{\partial(S_{TOA} - R_{TOA})}{\partial cloud} \frac{d(cloud)}{dT_S} + \frac{\partial(S_{TOA} - R_{TOA})}{\partial T_{air}} \frac{dT_{air}}{dT_S} \\
 &= \lambda_p + \lambda_{H_2O} + \lambda_{albedo} + \lambda_{cloud} + \lambda_{lapse\_rate} \\
 &= \lambda_p \{1 - (\lambda_{H_2O} + \lambda_{albedo} + \lambda_{cloud} + \lambda_{lapse\_rate}) / (-\lambda_p)\} \\
 &= \lambda_p \{1 - g_{H_2O} - g_{albedo} - g_{cloud} - g_{lapse\_rate}\}
 \end{aligned}$$

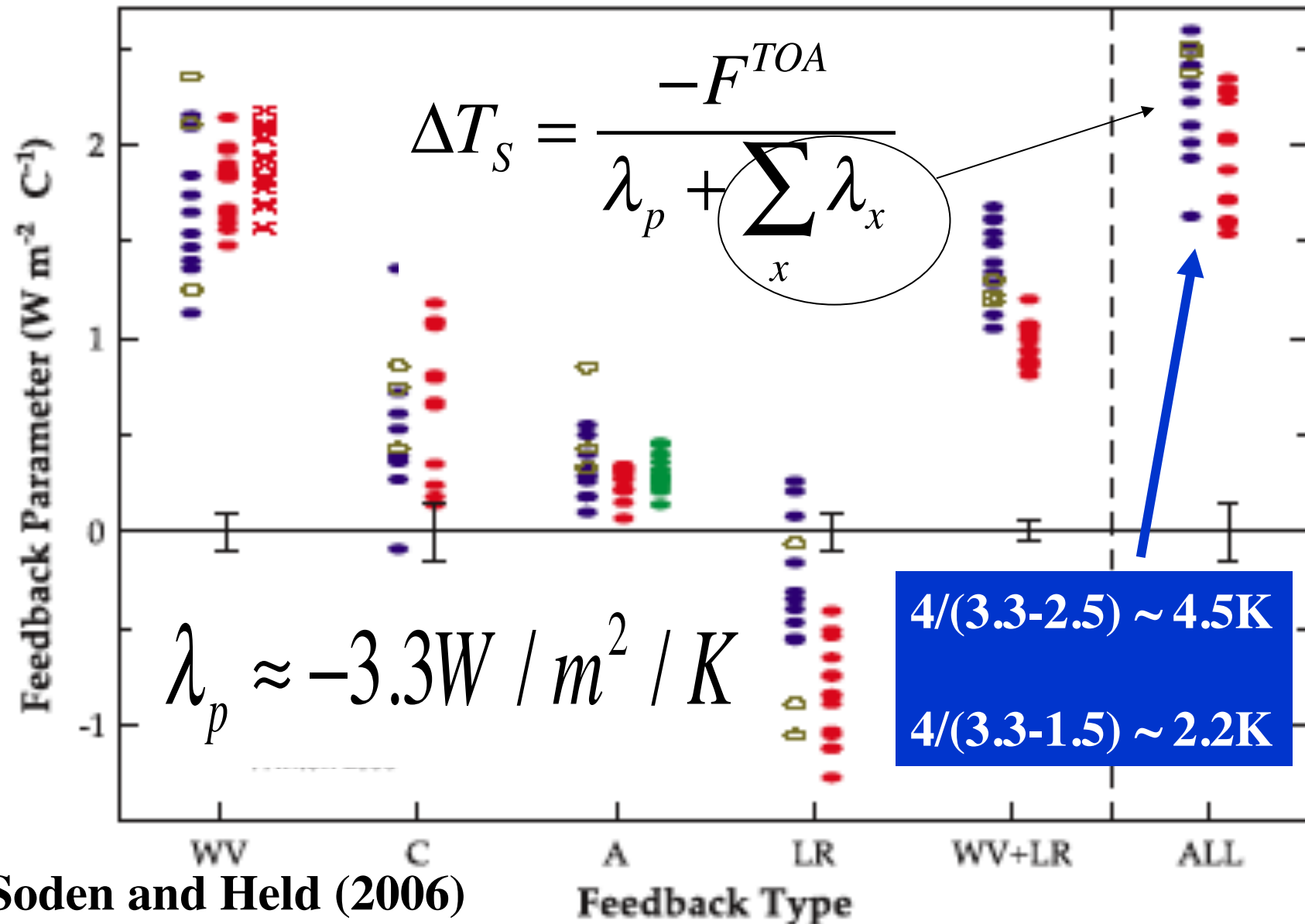
$$\Delta T_S = \frac{\Delta F^{TOA}}{-(\lambda_p + \sum_x \lambda_x)} = \frac{G_0 \Delta F^{TOA}}{1 - \sum_x g_x}$$

$$G_0 = -1 / \lambda_p : \text{initial gain}$$

$$G_{tot} = G_0 / (1 - \sum_x g_x) : \text{total gain}$$

Feedbacks are additive, but their effects are not!!

# Climate feedbacks and climate projection uncertainties (IPCC AR4)



Soden and Held (2006)

# Questions

- **Science:** What are the roles of atmospheric motions (turbulences, convections, large-scale motions) for the spatial (vertical and horizontal) variations of the warming pattern? Specifically, **can a change in the atmospheric circulation alone explain a larger warming in high latitudes?**
- **Technique:** How do we incorporate atmospheric dynamics in the climate feedback analysis?

# Why do we need to incorporate the dynamics into feedback analysis?

- **Atmospheric motions play a role in the climate response to the external forcing.**
- **Even for a global uniform SURFACE warming, local convection and surface evaporation and sensible heat fluxes would act to reduce surface warming while enhancing the atmospheric warming**

**It turns out they are hidden in the lapse rate feedback!!!**

# Coupled Atmosphere-Surface Climate Feedback-Response Analysis Method (CFRAM) for CGCM feedback analysis (Lu & Cai 2009; Cai & Lu 2009)

- **Forcing: an external perturbation profile in the atmosphere-surface column at each grid point**
- **Response: a vertically varying atmosphere-surface temperature profile at each grid point.**
- **Feedback: any energy flux perturbations that are not caused by the the longwave radiation change due to temperature changes.**

# Coupled Atmosphere-Surface Climate Feedback-Response Analysis Method (CFRAM) for CGCM feedback analysis

Lu and Cai (2008) and Cai and Lu (2008)

## Unperturbed climate state

$$\underbrace{(\bar{S} - \bar{R})}_{\text{net rad. cooling/heating}} + \underbrace{\bar{Q}}_{\text{non-radiative dyn. heating/cooling}} = \frac{\partial \vec{E}}{\partial t}$$

## Perturbation in response an external forcing

$$\underbrace{\Delta(\bar{S} - \bar{R})}_{\text{change in net rad. cooling/heating (F}^{2\text{CO}_2}\text{ included)}} + \underbrace{\Delta\bar{Q}}_{\text{change in non-radiative dyn. heating/cooling}} = \underbrace{\Delta\vec{E}}_{\text{Heat Storage}}$$

# Mathematical formulation of CFRAM

$$\left( \frac{\partial \bar{\mathbf{R}}}{\partial \bar{\mathbf{T}}} \right) \Delta \bar{\mathbf{T}}^{tot} = \left\{ \bar{\mathbf{F}}^{ext} + \underbrace{\Delta^{(\alpha)} \bar{\mathbf{S}} + \Delta^{(c)} (\bar{\mathbf{S}} - \bar{\mathbf{R}}) + \Delta^{(w)} (\bar{\mathbf{S}} - \bar{\mathbf{R}})}_{non\_temp\_induced\_radiative\_energy} + \underbrace{\Delta \bar{\mathbf{Q}}}_{non-radiative\_energy} - \underbrace{\Delta \bar{\mathbf{E}}}_{Heat\ Storage} \right\}$$

The radiation flux change only due to a change in the atmosphere-surface column temperature

= Radiative energy input due to the external forcing +

$\left( \frac{\partial \bar{\mathbf{R}}}{\partial \bar{\mathbf{T}}} \right)$  Planck feedback matrix

**Radiative** and **non-radiative** energy flux perturbations that are not due to the radiation change associated with temperature changes and external forcing



# Mathematical formulation of CFRAM

$$\Delta \bar{\mathbf{T}}^{tot} = \left( \frac{\partial \bar{\mathbf{R}}}{\partial \bar{\mathbf{T}}} \right)^{-1} \left\{ \bar{\mathbf{F}}^{2CO_2} + \Delta^{(\alpha)} \bar{\mathbf{S}} + \Delta^{(c)} (\bar{\mathbf{S}} - \bar{\mathbf{R}}) + \Delta^{(w)} (\bar{\mathbf{S}} - \bar{\mathbf{R}}) + \Delta \bar{\mathbf{Q}} - \Delta \bar{\mathbf{E}} \right\}$$

$$-\Delta^{total} (\bar{\mathbf{S}} - \bar{\mathbf{R}}) = \Delta \bar{\mathbf{Q}} - \Delta \bar{\mathbf{E}} = \Delta \bar{\mathbf{Q}}^{evaporation} + \Delta \bar{\mathbf{Q}}^{surface\_sensibl\_heat+flux} + (\Delta \bar{\mathbf{Q}}^{convection} + \Delta \bar{\mathbf{Q}}^{ATM\_lg\_dyn}) + \Delta \bar{\mathbf{Q}}^{OCN\_dyn+storage}$$

$$\Delta \bar{\mathbf{T}}^{(n)} = \left( \frac{\partial \bar{\mathbf{R}}}{\partial \bar{\mathbf{T}}} \right)^{-1} \Delta \bar{\mathbf{F}}^{(n)}$$

$$\Delta \bar{\mathbf{T}}^{tot} = \sum_n \Delta \bar{\mathbf{T}}^{(n)}$$

**Both feedbacks and their effects are additive!**

# Demonstration of the Dynamical PWA mechanism in a GCM without hydrological cycle

(Lu and Cai 2010; Cai and Tung 2012)

**The science question:**

**Can the surface warming in response to anthropogenic greenhouse gases be still stronger in high latitudes than in low latitudes in the absence of **ice-albedo** and **evaporation** feedbacks, and **poleward latent heat transport** in a **GCM** model?**

# The key features of the coupled GCM model

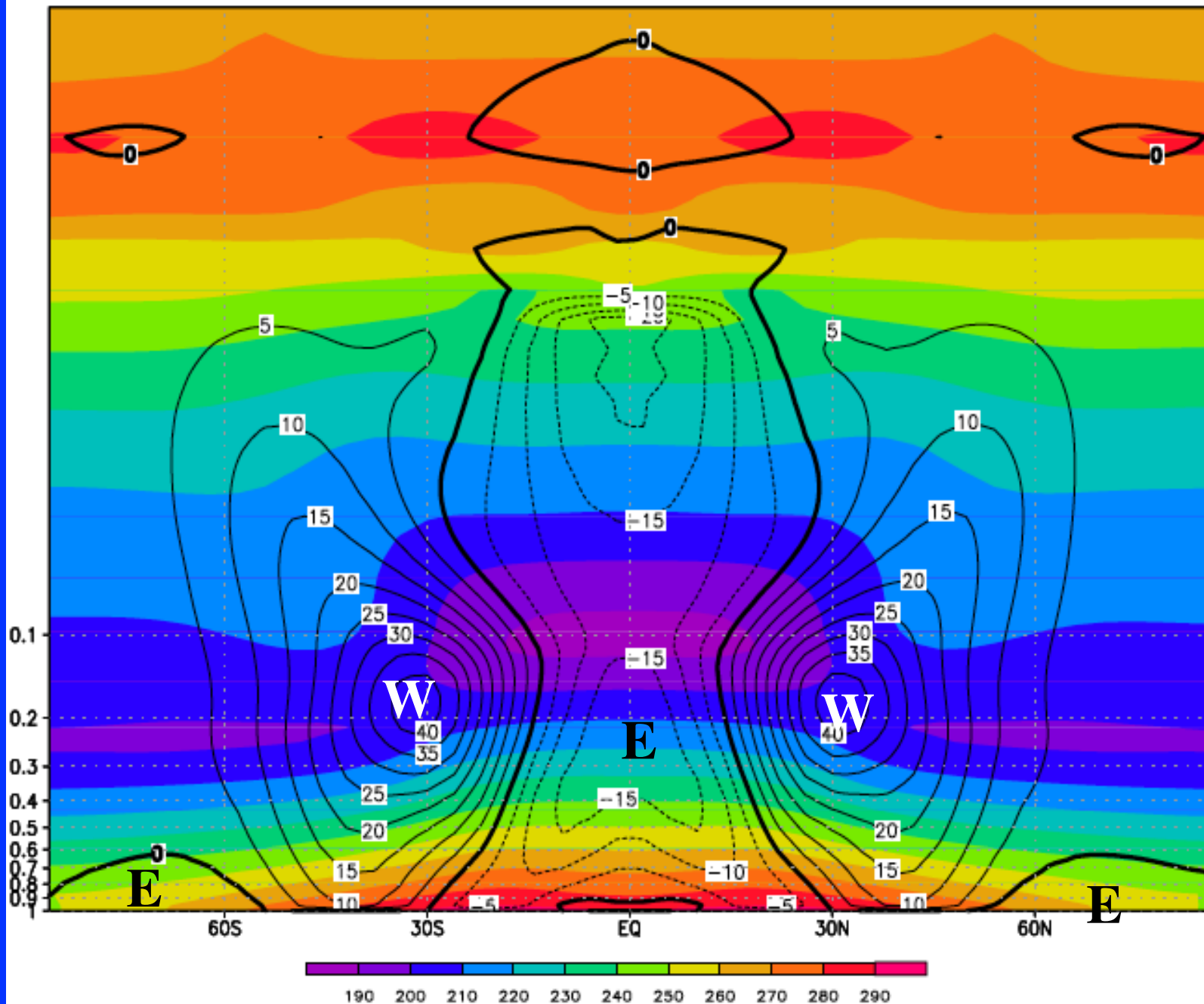
**Dynamical core: Suarez and Held (1992)**

**Physics:**

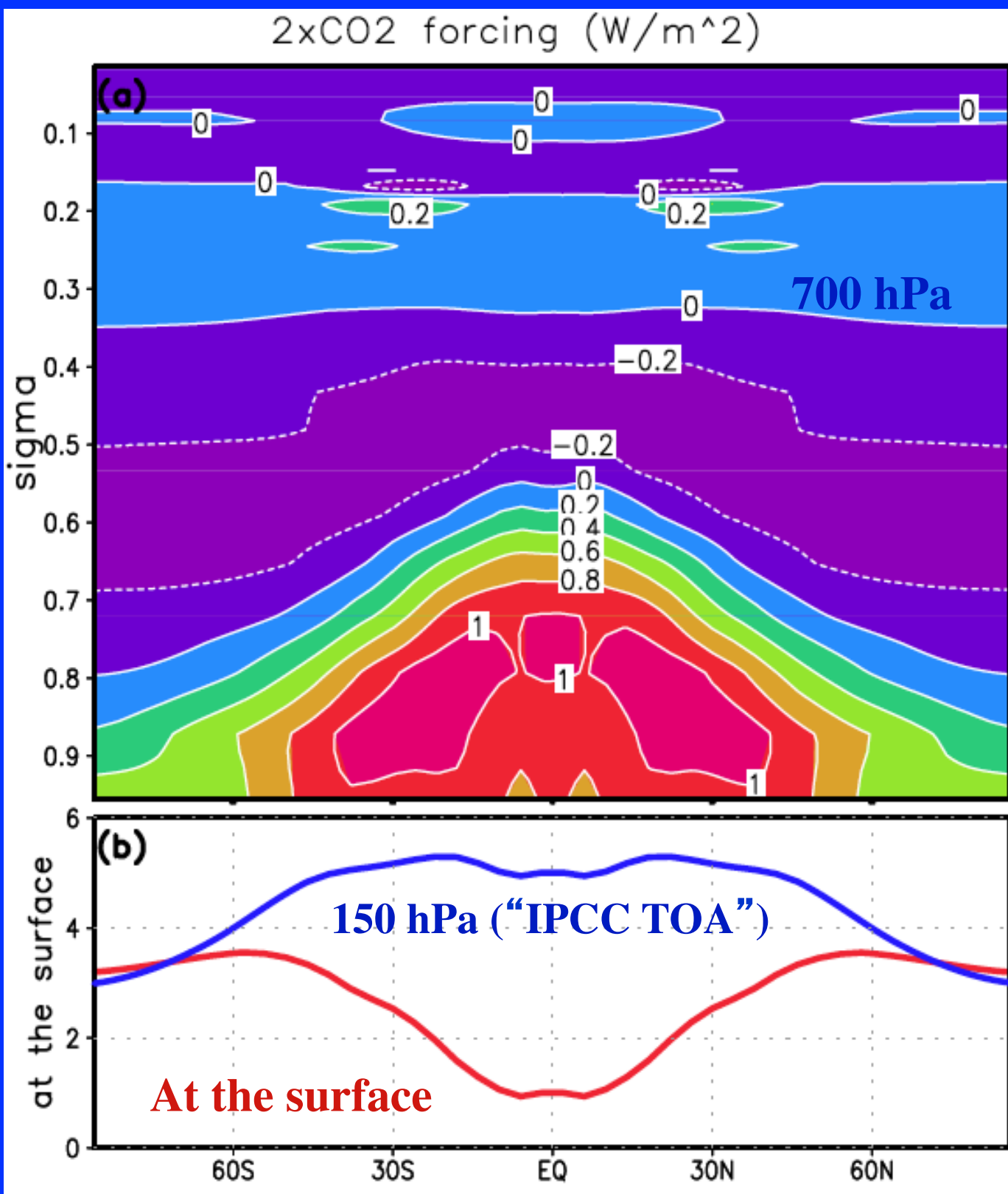
- **Fu et al. (1992)' s radiation model.**
- **Dry convection adjustment so that maximum lapse rate cannot exceed a preset meridional profile (6.5K/1km in tropics and 9.8K/1km outside).**
- **Atmospheric relative humidity is kept at a prescribed vertical and meridional profile.**
- **The surface energy balance model that exchanges sensible heat flux, emits long wave radiation out, and absorbs downward radiation at the surface.**
- **The annual mean solar forcing.**
- **1CO<sub>2</sub> versus 2CO<sub>2</sub> climate simulations**

# Climatology of the GCM

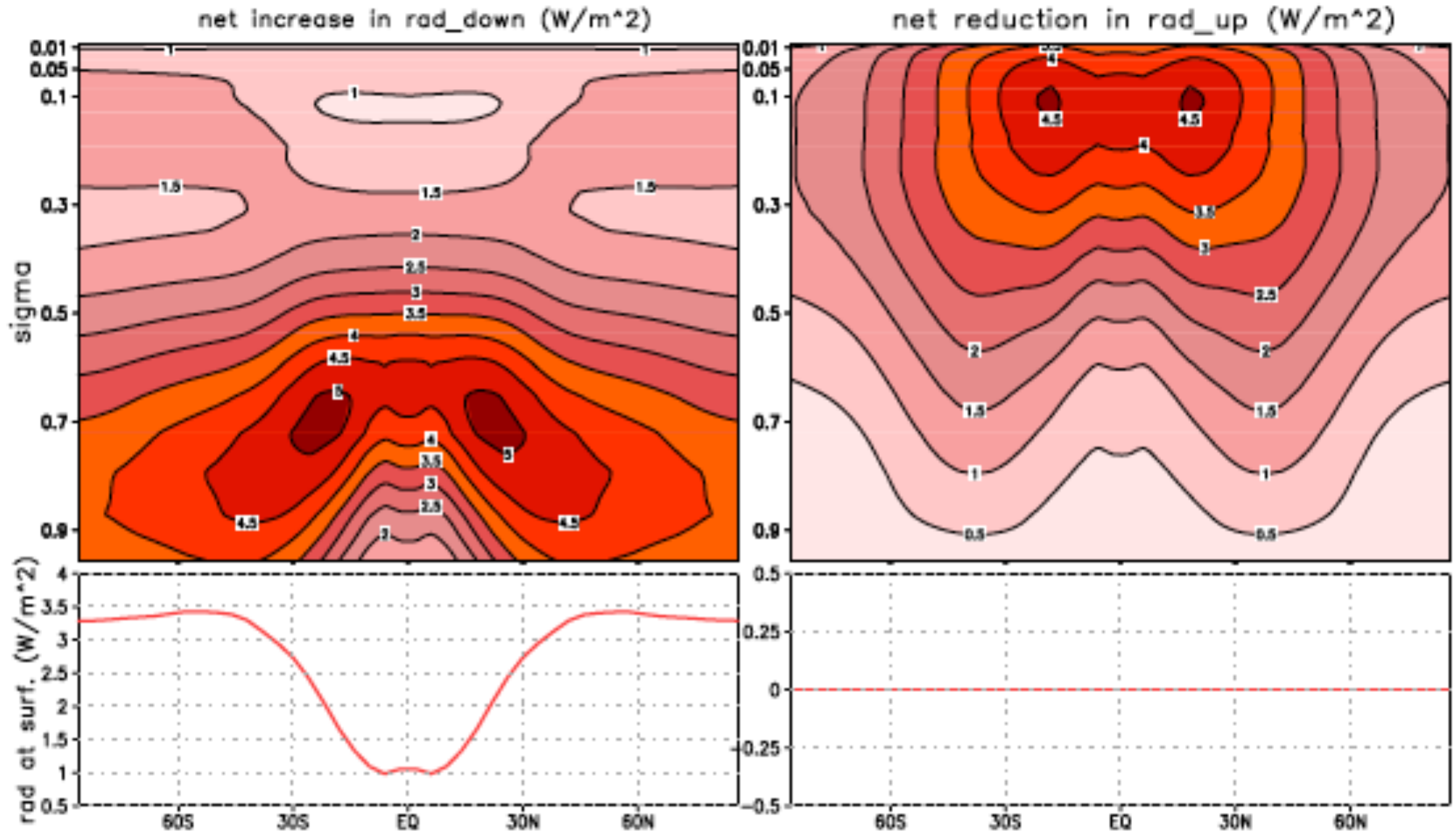
[T] and [U] in the control run



# 2CO<sub>2</sub> Climate forcing (w/m<sup>2</sup>)



# Changes in upward and downward LW radiative energy flux due 2xCO<sub>2</sub>



## Total Warming Pattern

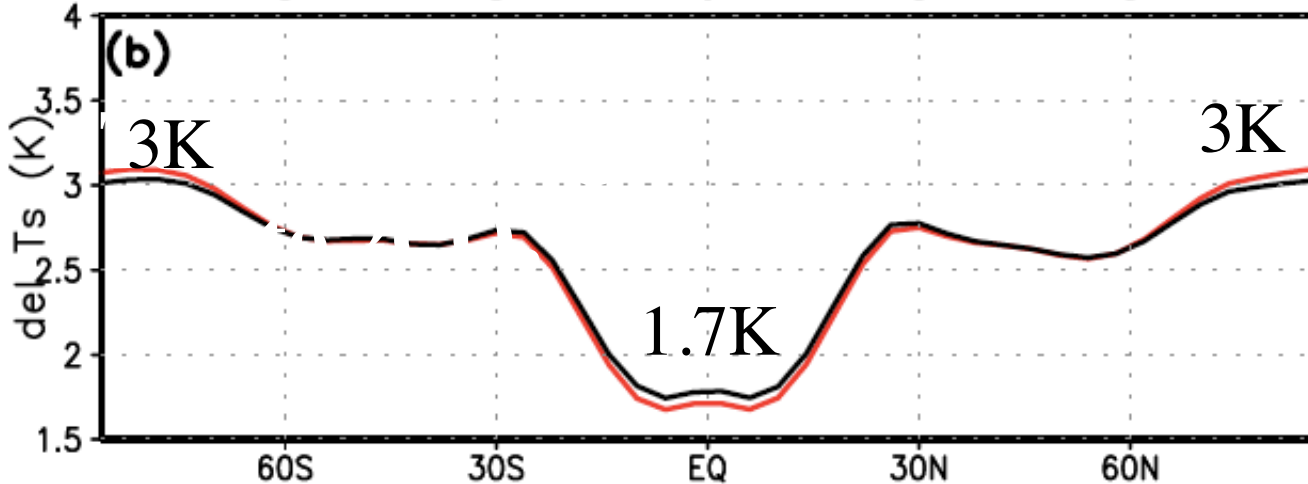
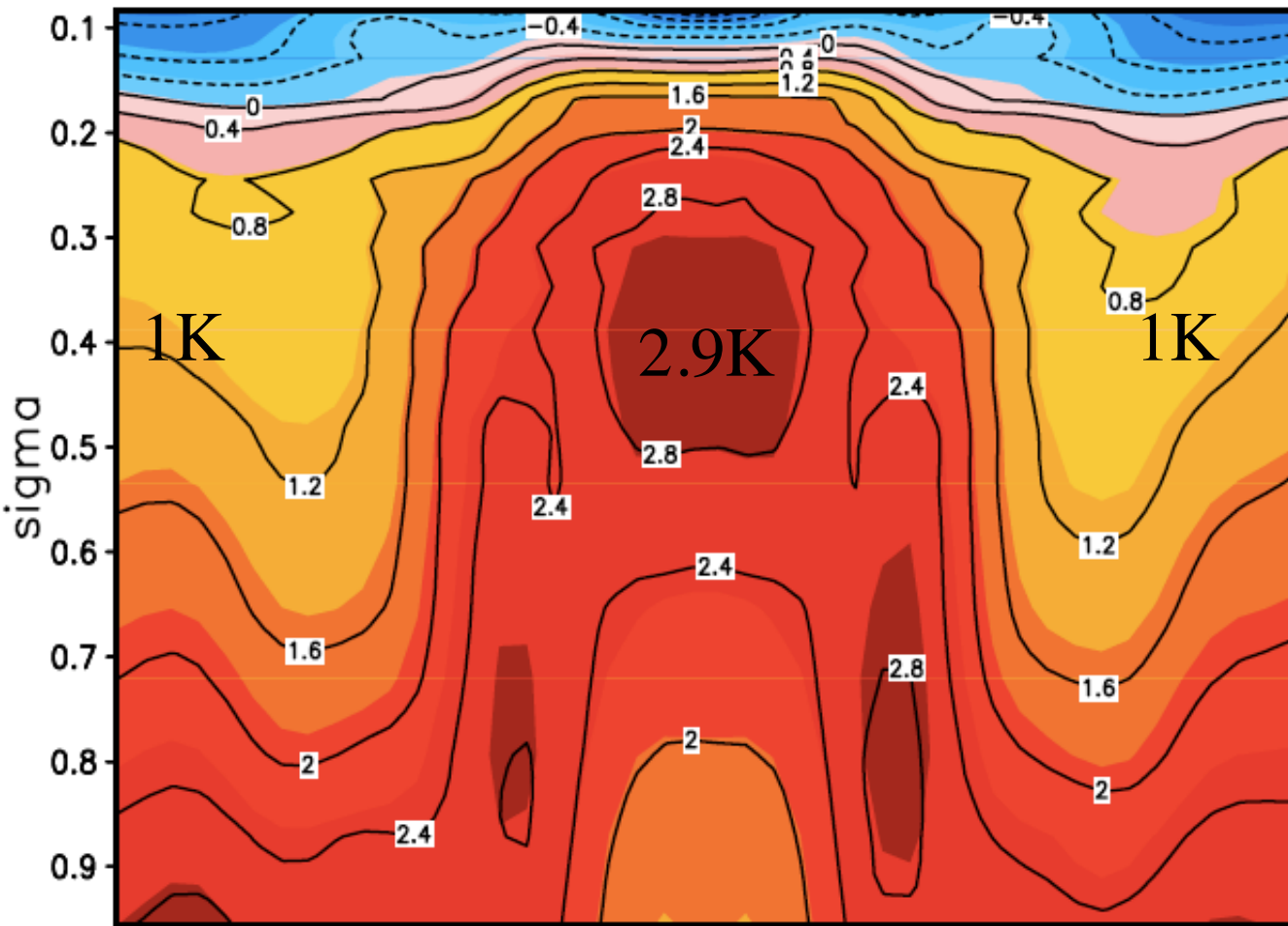
1. In the atmosphere:  
 $\Delta T(\text{trop}) > \Delta T(\text{polar})$

2. At the surface:  
 $\Delta T(\text{trop}) > \Delta T(\text{polar})$

3. In the tropics:  
 $\Delta T_{\text{surf}} < \Delta T_{\text{air}}$

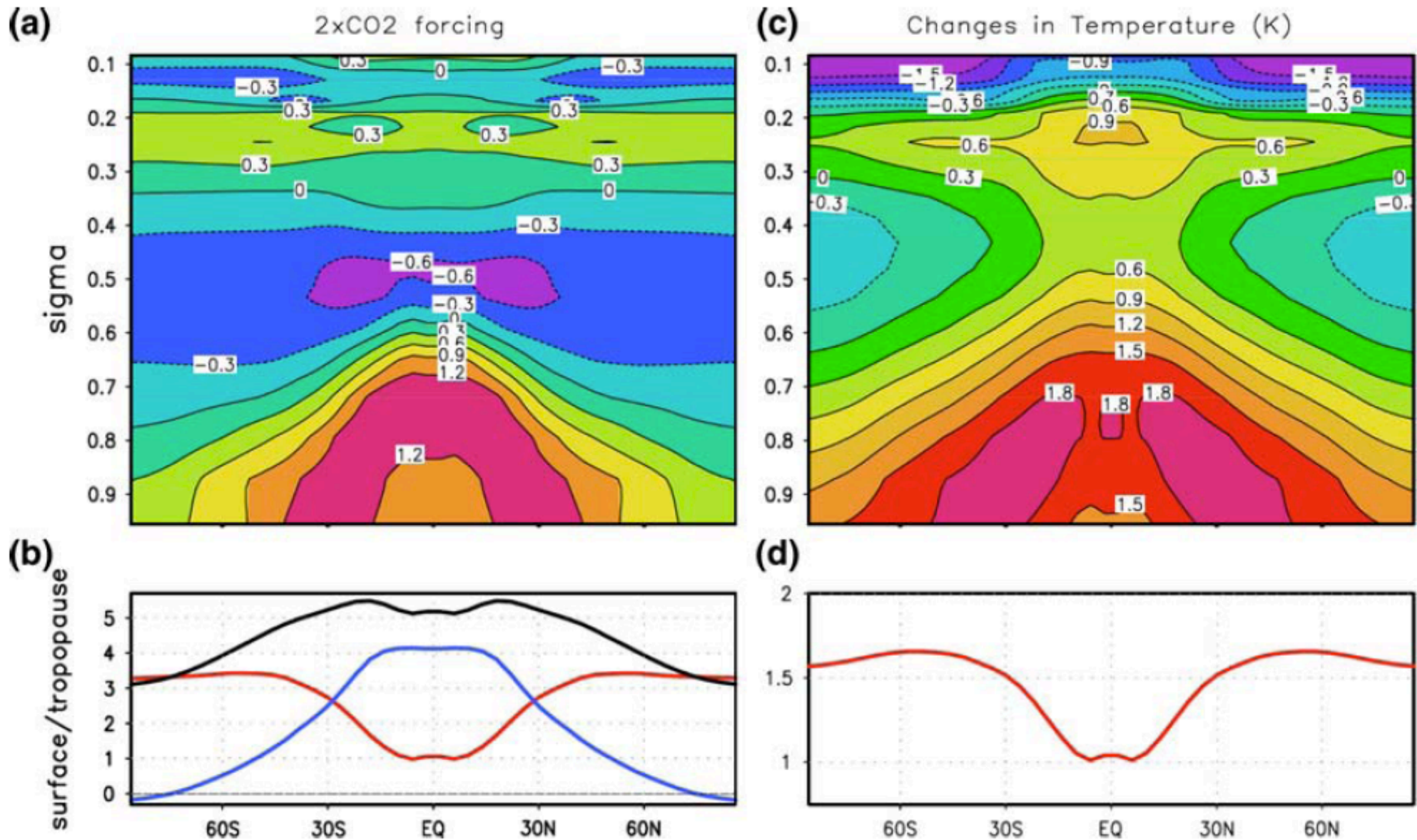
4. In polar region:  
 $\Delta T_{\text{surf}} > \Delta T_{\text{air}}$

(a)  $d_{\text{Ta}}$  (K), 6-lat. moist adiabat



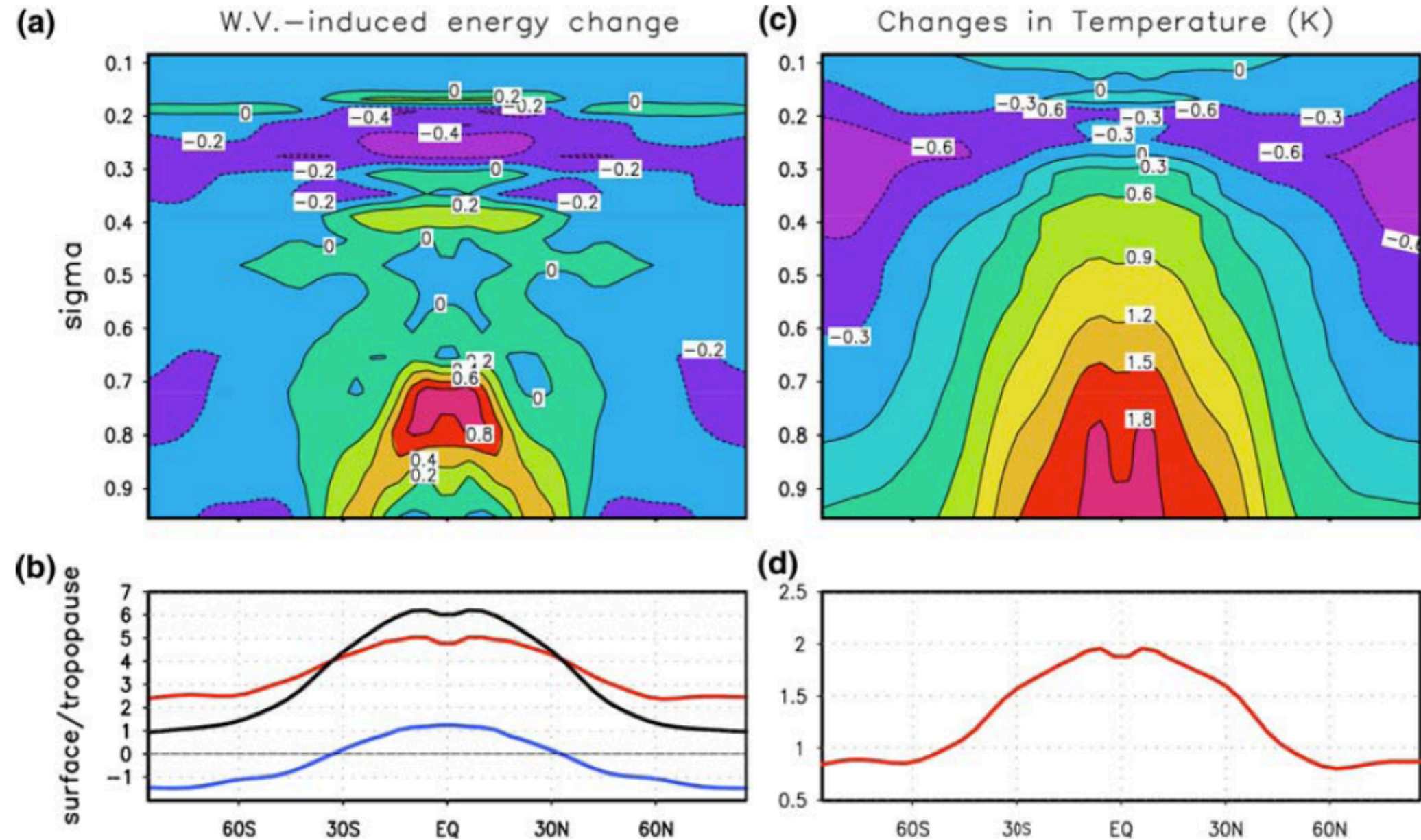


# Temp. Changes due to 2xCO<sub>2</sub> Alone

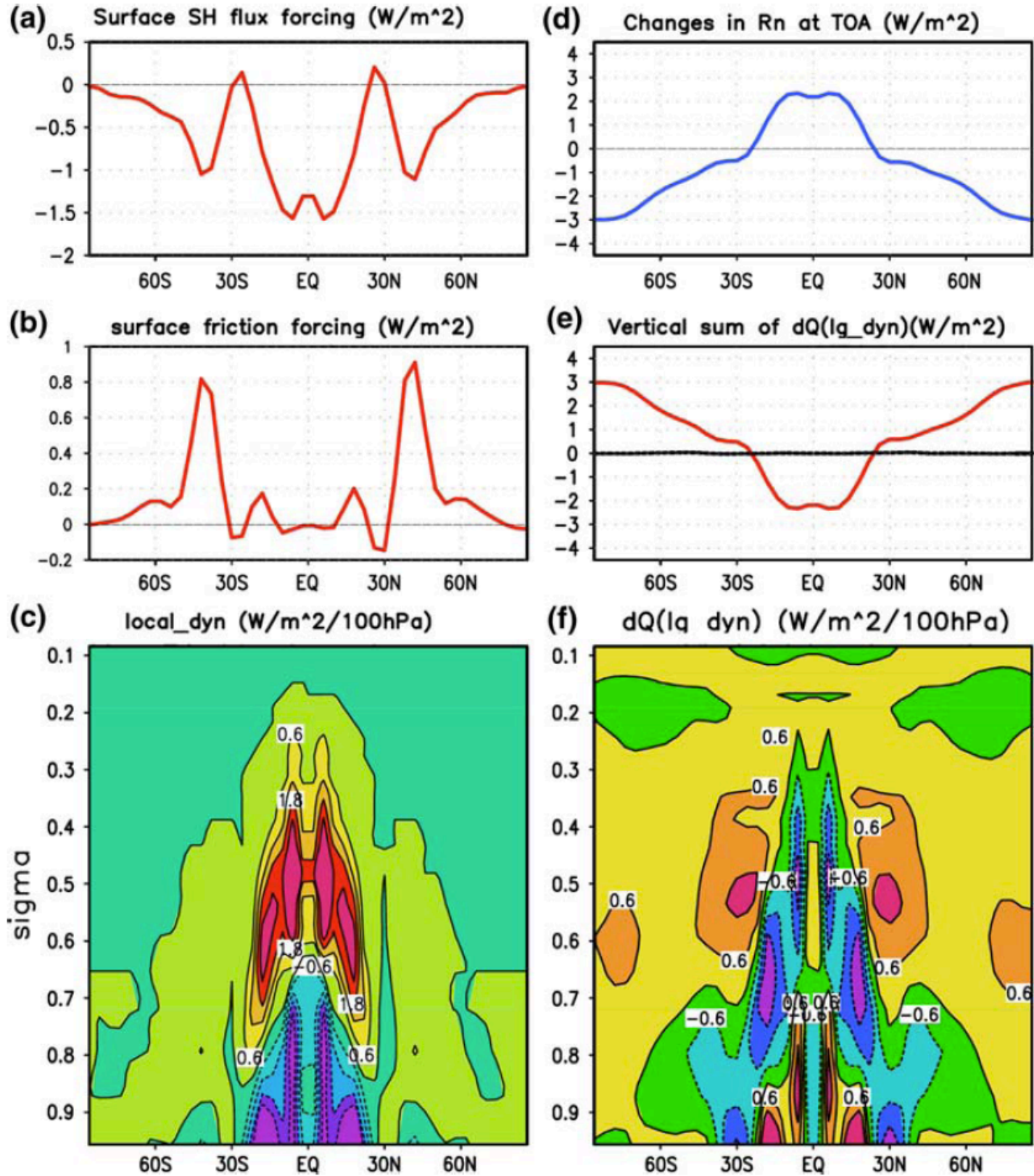




# Temp. Changes due to WV feedback Alone

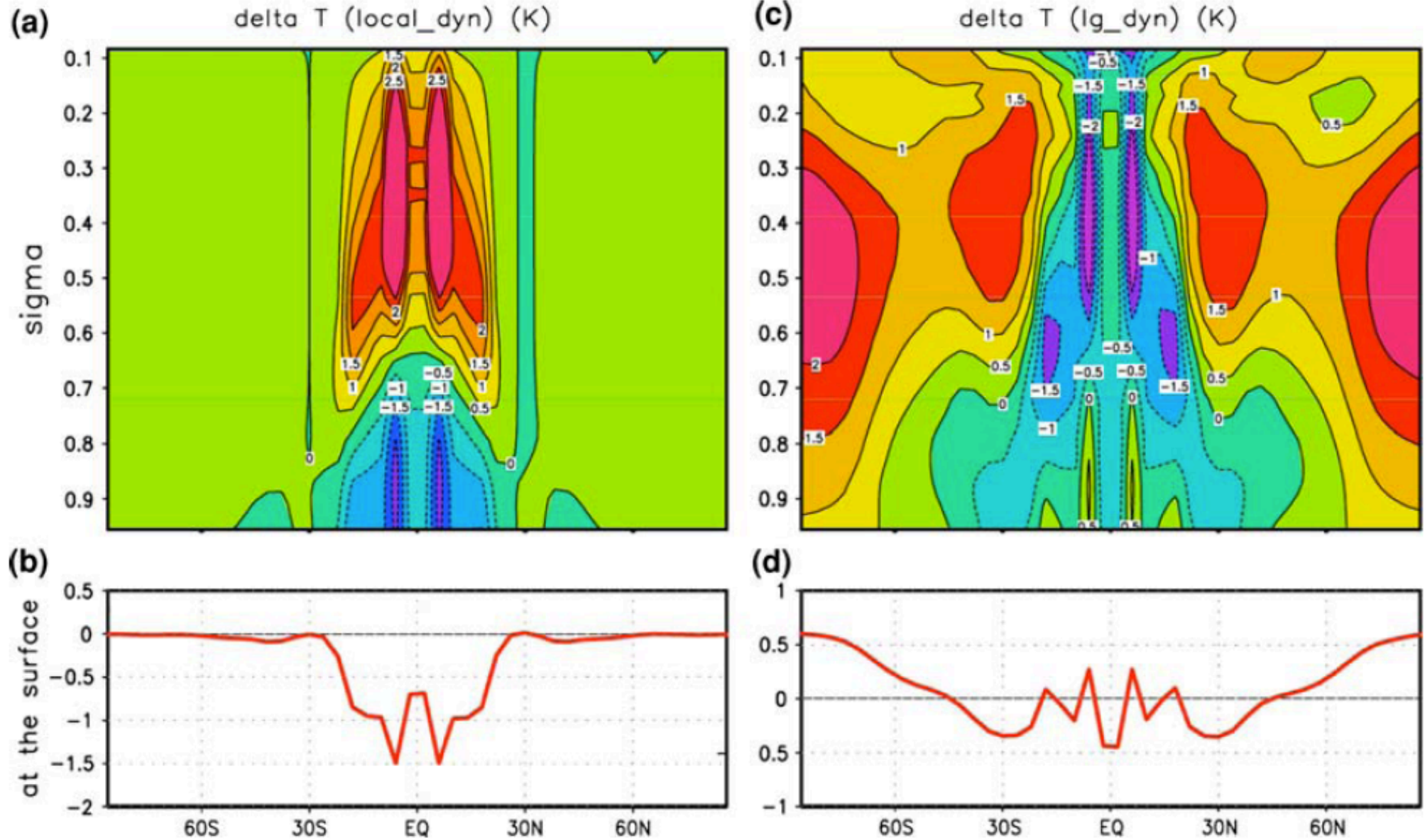


# Changes in non-radiative energy fluxes

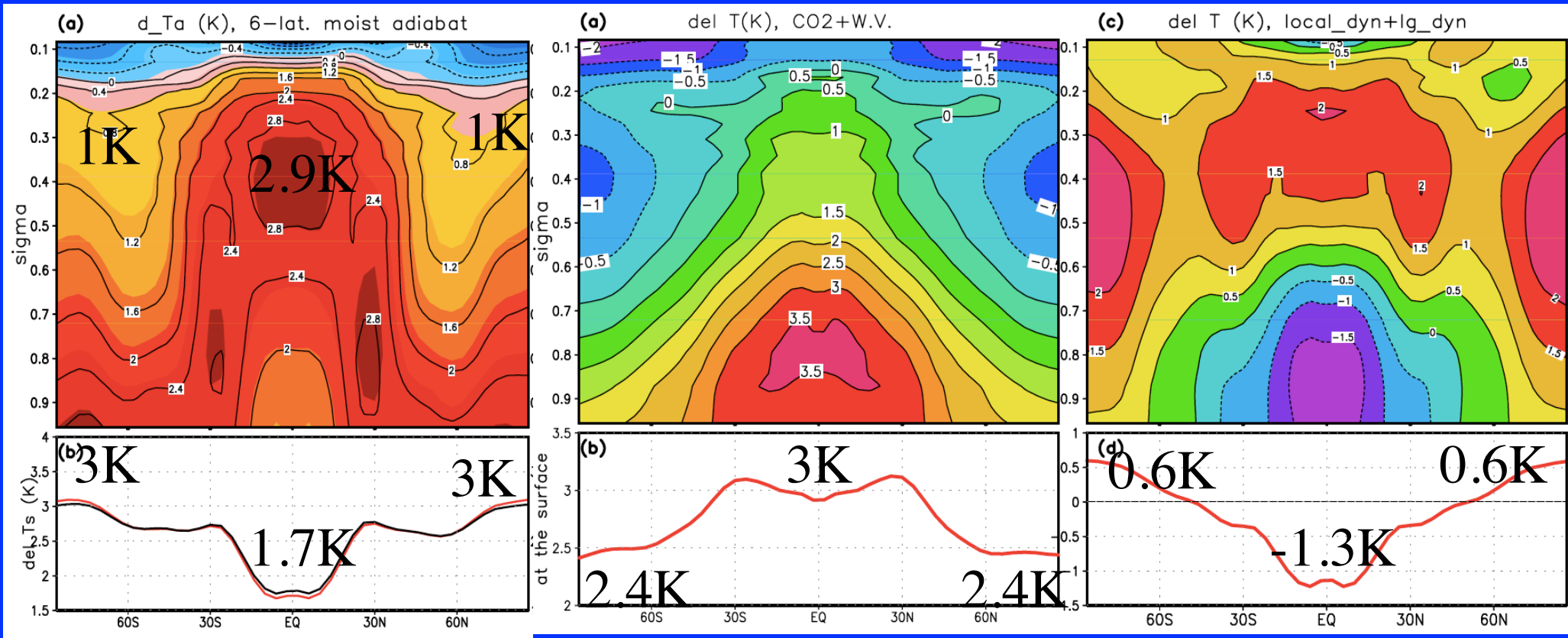




# Temp. Changes due to non-radiative conv. & large-scale dyn. feedbacks



# Total warming and Sum of partial $\Delta T$ s



Total warming  
due to 2CO<sub>2</sub>

2CO<sub>2</sub> + H<sub>2</sub>O)  
feedbacks

Convective  
+ Poleward  
energy  
transport  
feedbacks<sup>32</sup>

# Summary of “dry” GCM results

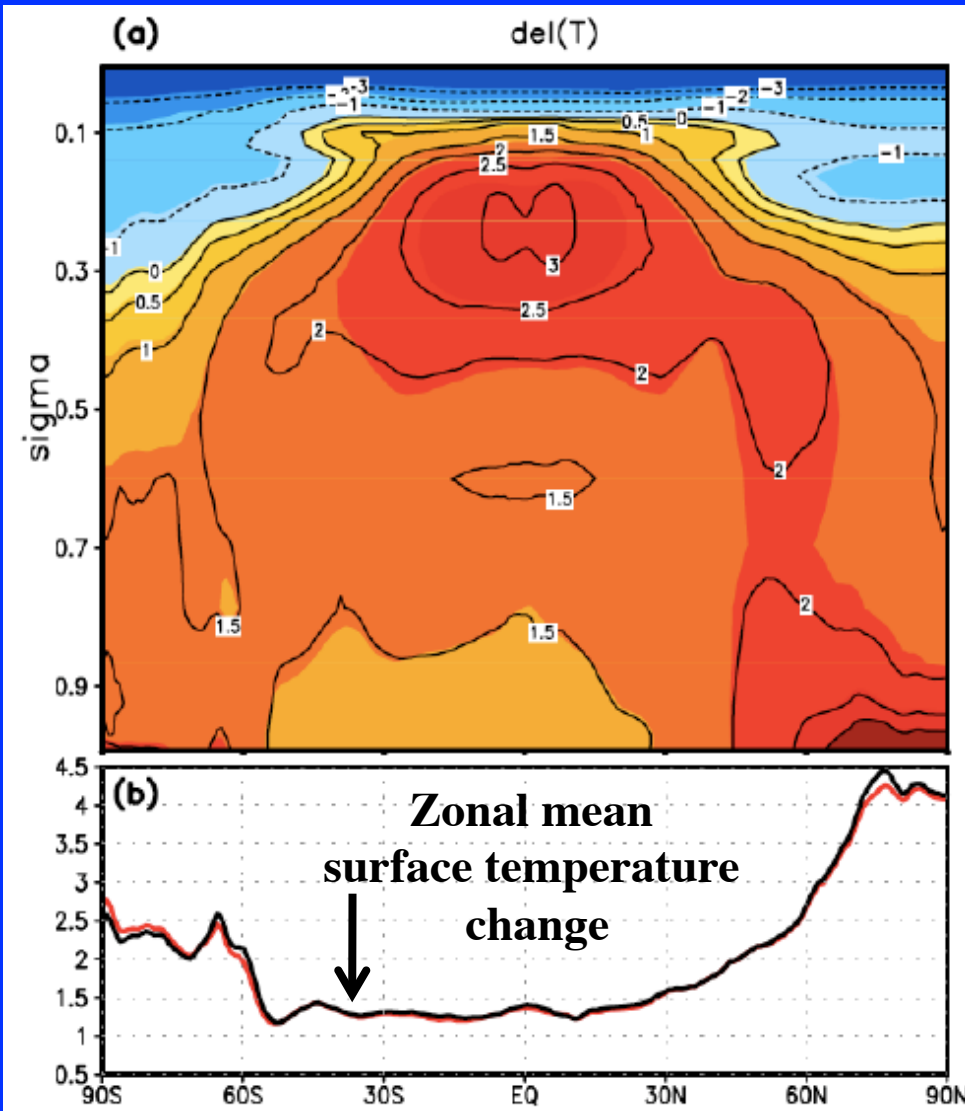
- **2CO<sub>2</sub> forcings exhibits a poleward and vertical decreasing profile in the atmosphere.**
- **The water vapor feedback strengthens the upward decreasing radiative heating profile in the tropics and the poleward decreasing radiative heating profile in the lower troposphere.**
- **The convective feedback plays an important role only in the tropics where they act to reduce the warming at the surface and lower troposphere in favor of upper troposphere warming.**
- **The large-scale dynamical poleward energy transport is enhanced in both cases, contributing to a polar amplification of warming aloft and a warming reduction in the tropics.**
- **The dynamical amplification of polar atmospheric warming also contributes additional warming to the surface below via downward thermal radiation.**

# NCAR NCAR CCSM4 Climate Simulations

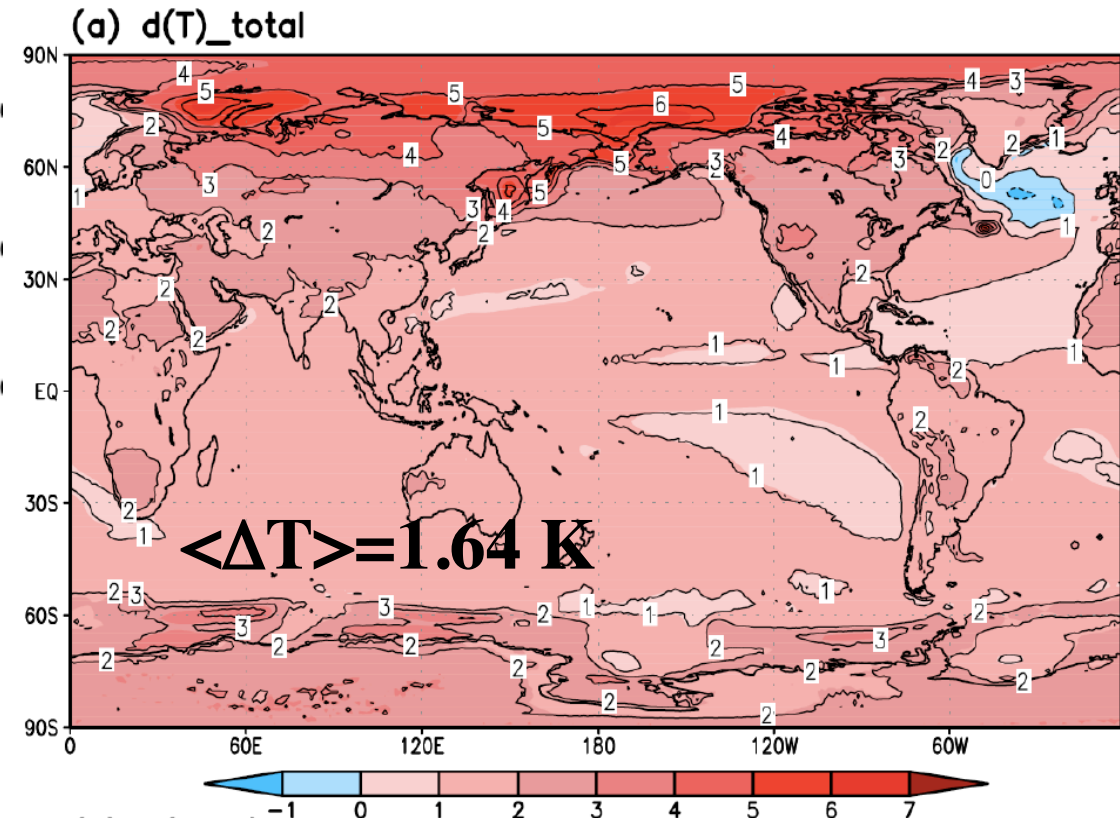
(Taylor et al. 2013, J. of Climate)

# Temperature Response to 2xCO<sub>2</sub> Forcing in NCAR CCSM4 Climate Simulations

(at the time of doubling of CO<sub>2</sub> from its pre-industry level 284.7 PPM)



**Zonal mean**  
← **air temperature change**      **surface change** ↓



# Questions

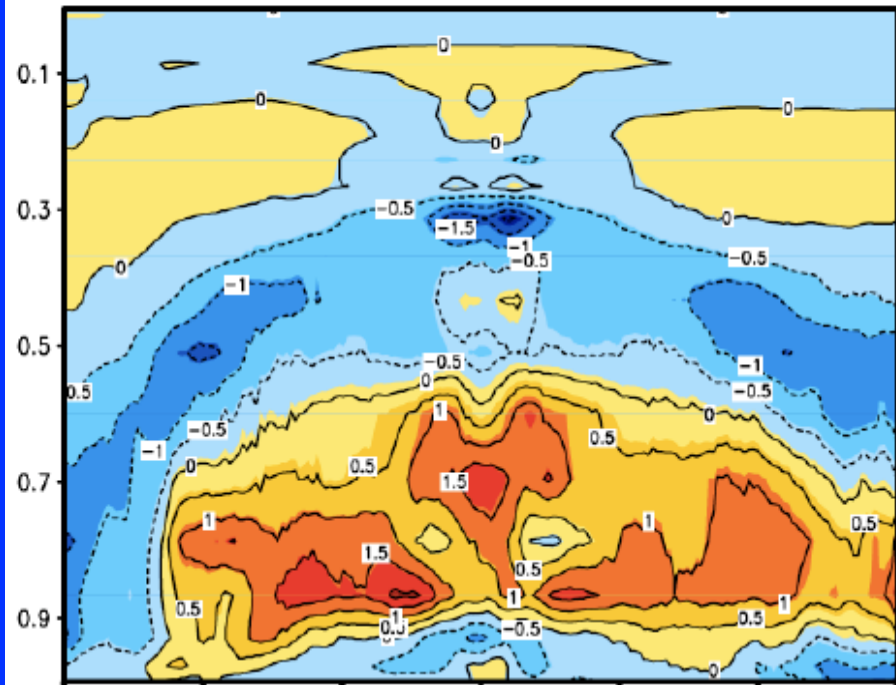
- **How much warming is just due to the doubling of CO<sub>2</sub> alone?**
- **What are the additional temperature changes due to various radiative and non-radiative feedback processes?**
- **What are their contributions to the final warming pattern?**
- **What are the main processes contributing the polar warming amplification?**



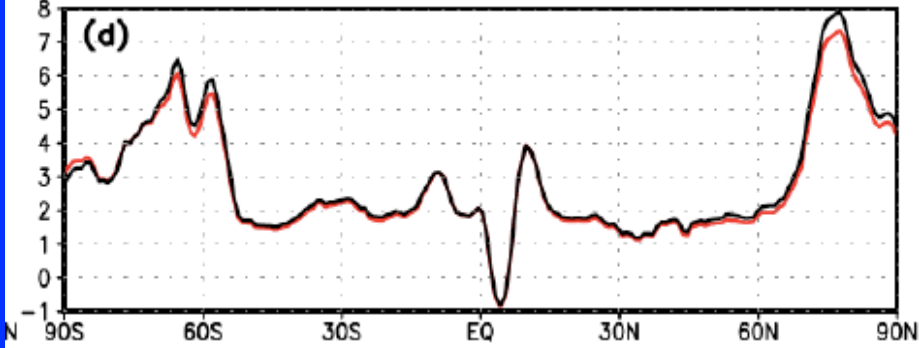
# Validation of Linearization

$$\underbrace{\Delta^{(tot)}(\bar{S} - \bar{R})}_{\text{Shadings}} \approx \underbrace{\bar{F}^{2CO_2} + \Delta^{(\alpha)}\bar{S} + \Delta^{(c)}(\bar{S} - \bar{R}) + \Delta^{(w)}(\bar{S} - \bar{R})}_{\text{contours}} - \left( \frac{\partial \bar{R}}{\partial \bar{T}} \right) \Delta \bar{T}^{tot}$$

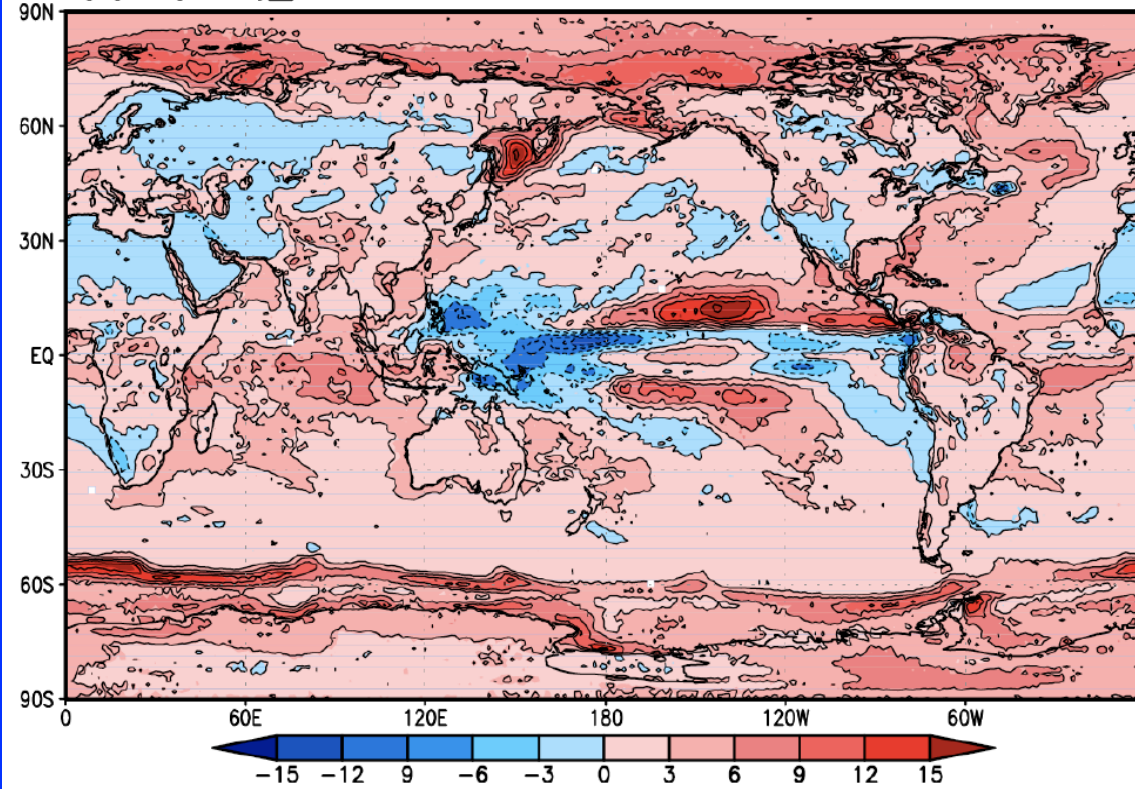
(c) del(S-R)



(d)



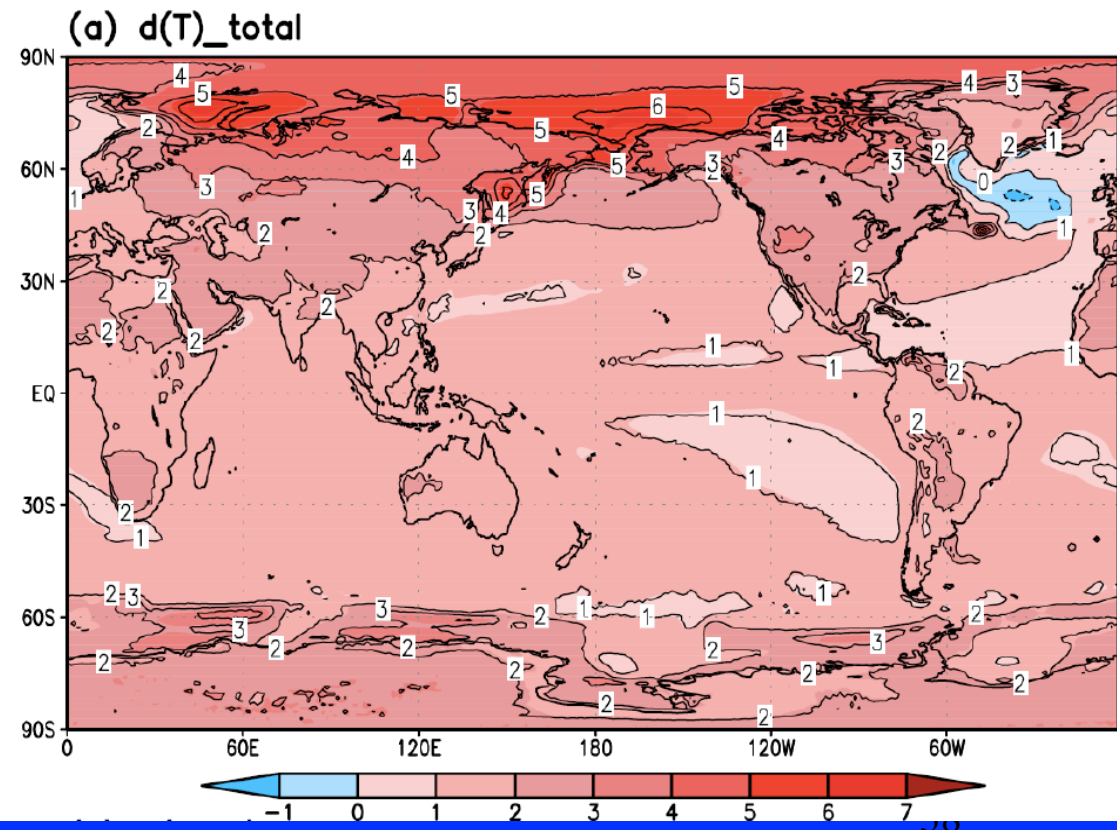
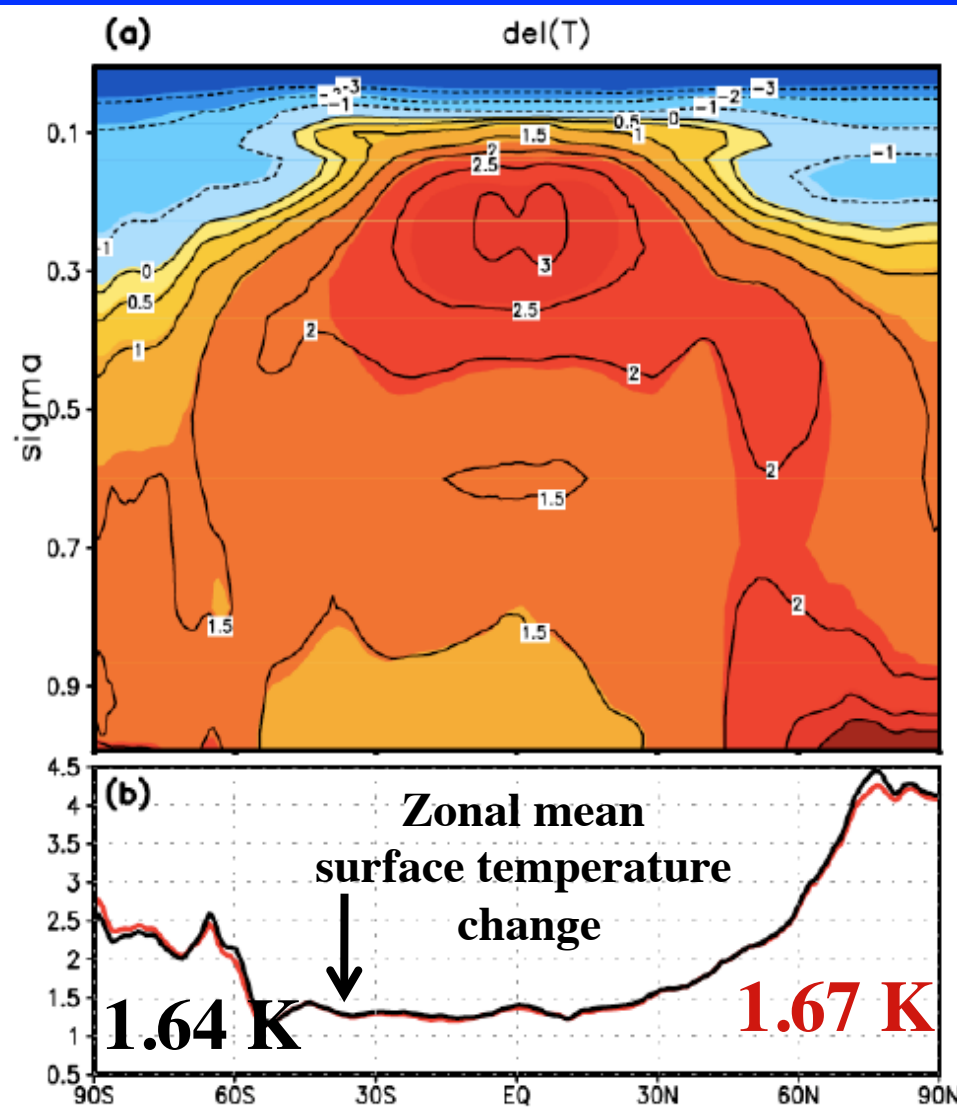
(b) d(S-R)\_total



# Validation of CFRAM:

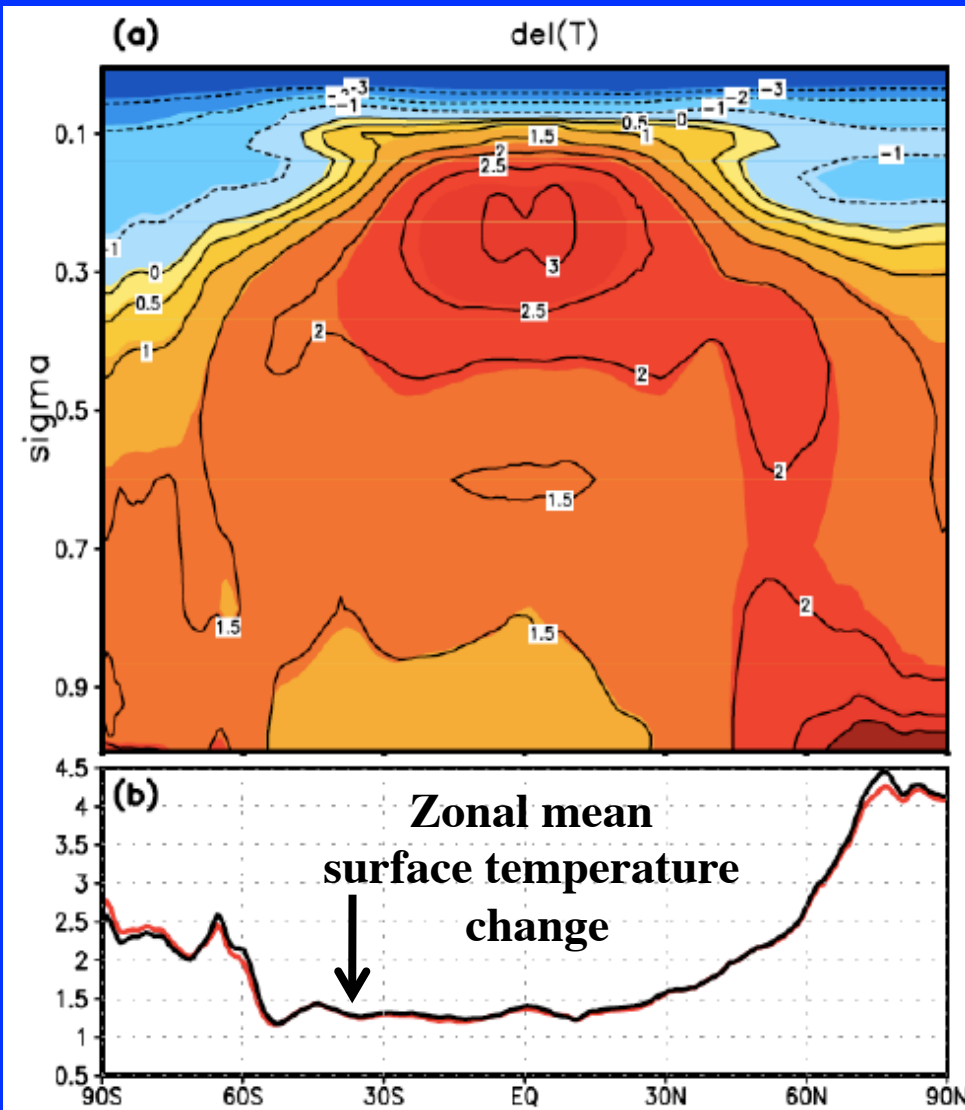
$$\Delta T^{tot} = \sum_n \Delta T^{(n)}$$

Zonal mean  
air temperature  
change ← surface  
change ↓

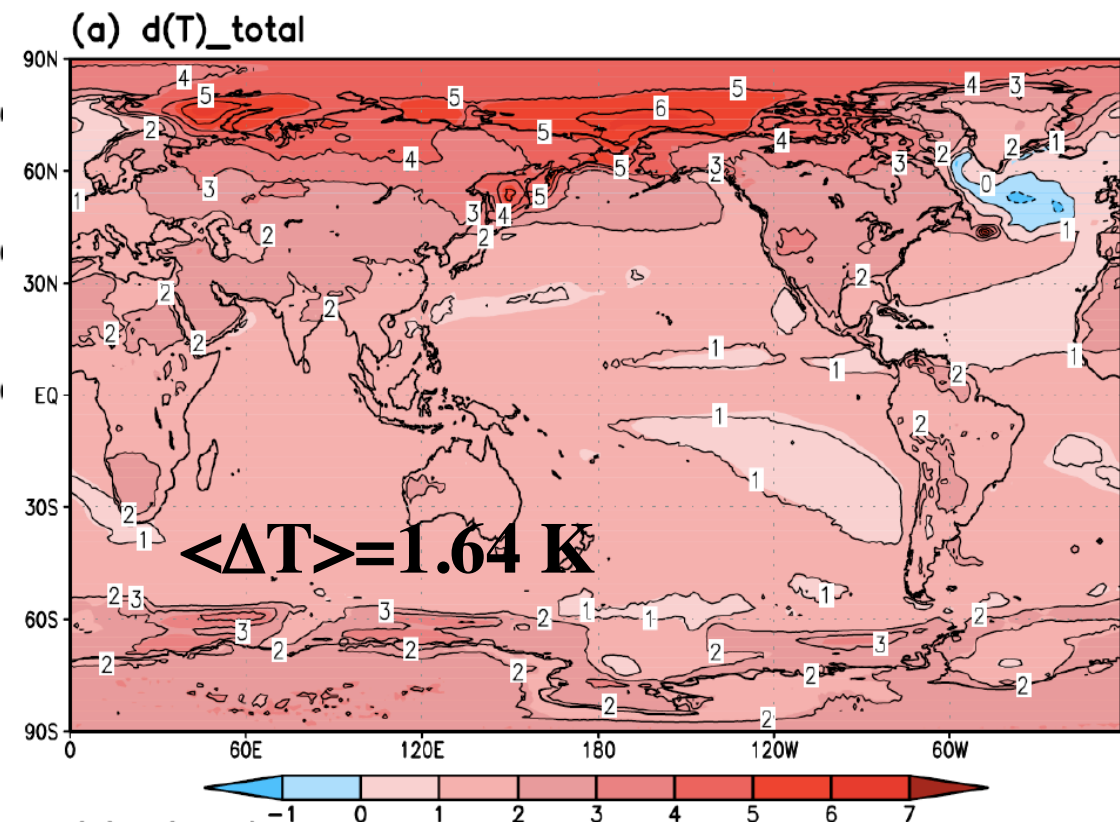


# Temperature Response to 2xCO<sub>2</sub> Forcing in NCAR CCSM4 Climate Simulations

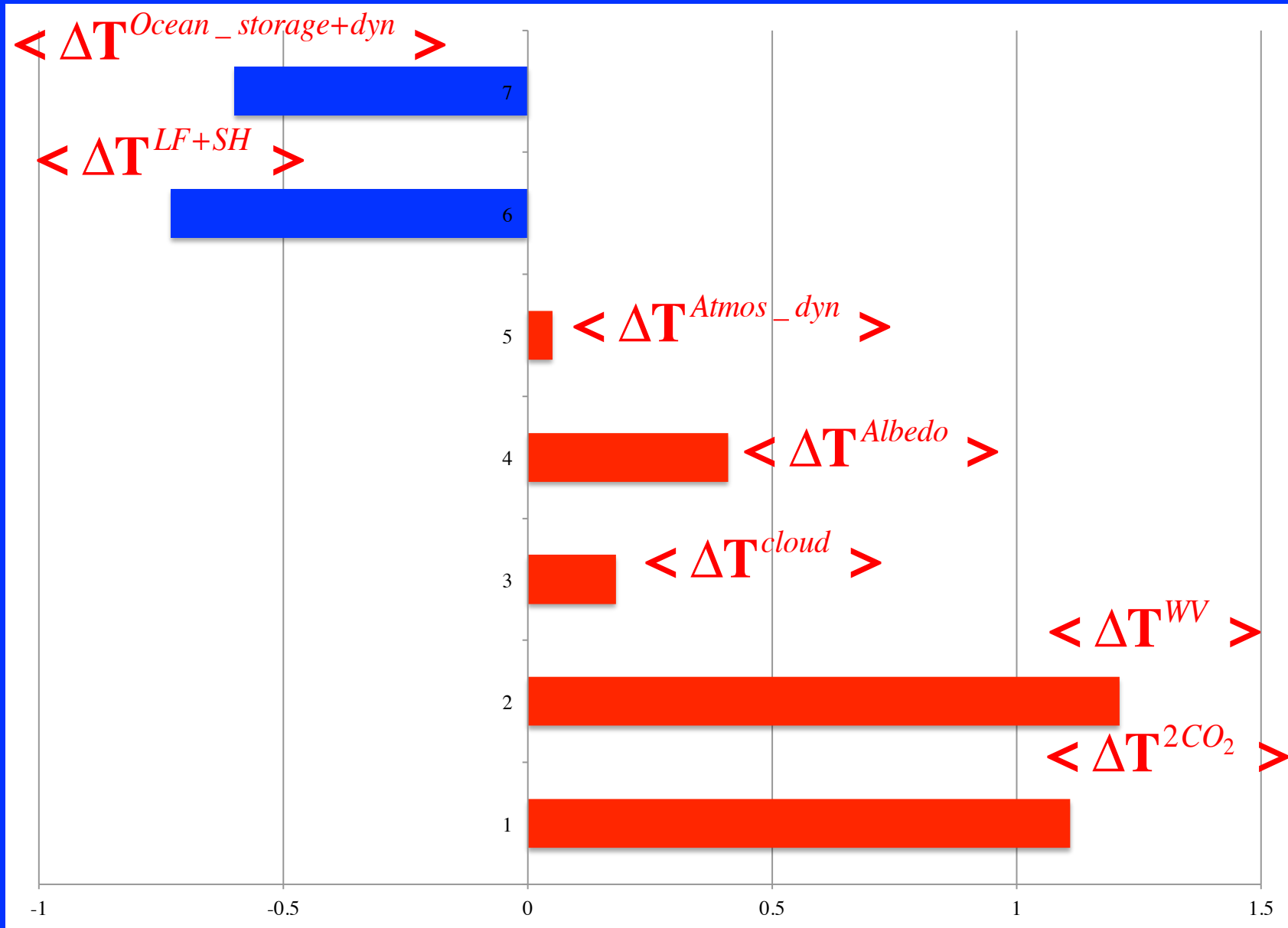
(at the time of doubling of CO<sub>2</sub> from its pre-industry level 284.7 PPM)



**Zonal mean**  
← **air temperature change**      **surface change** ↓



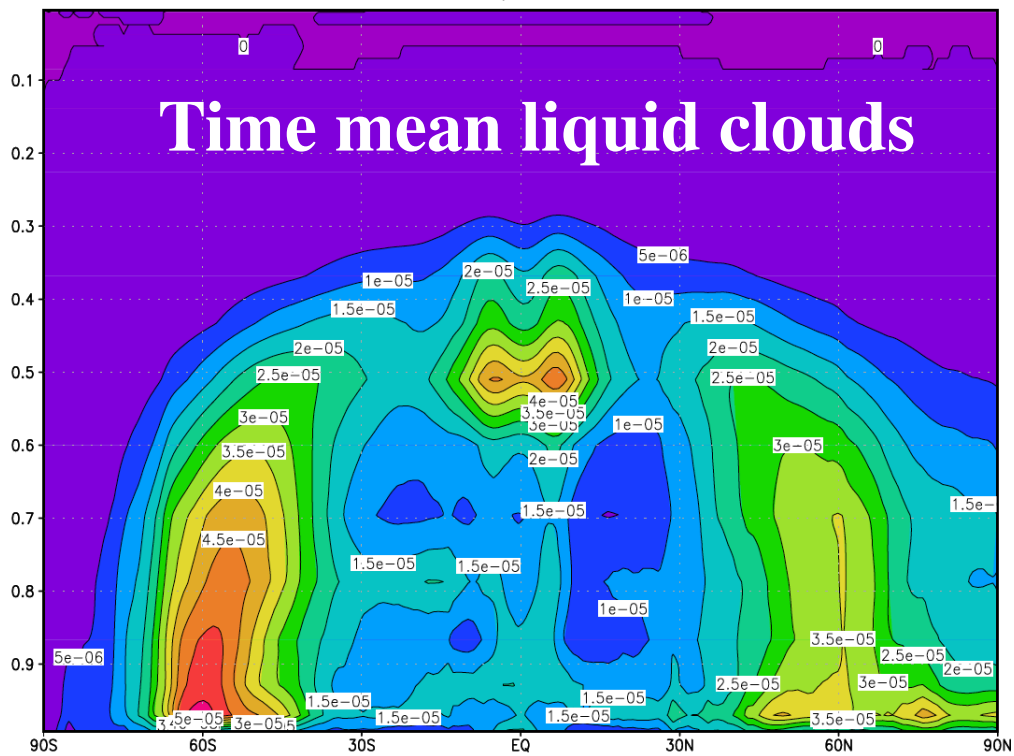
# Global Mean Surf. Temp. Changes



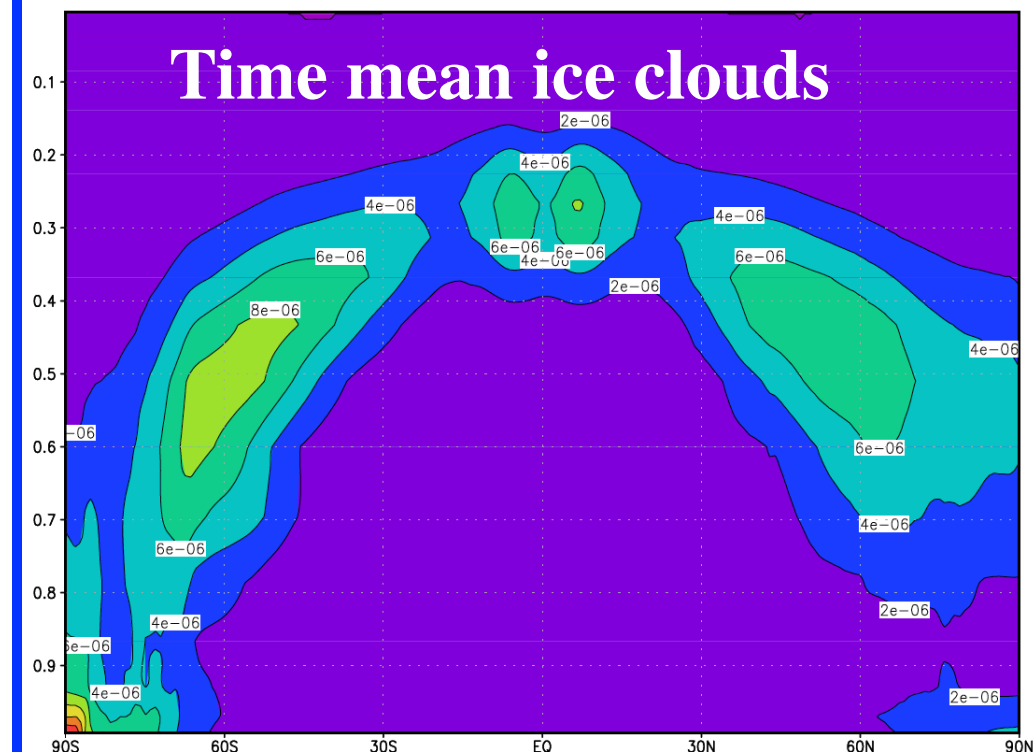
Global mean equilibrium response should be somewhat larger than 2.2K



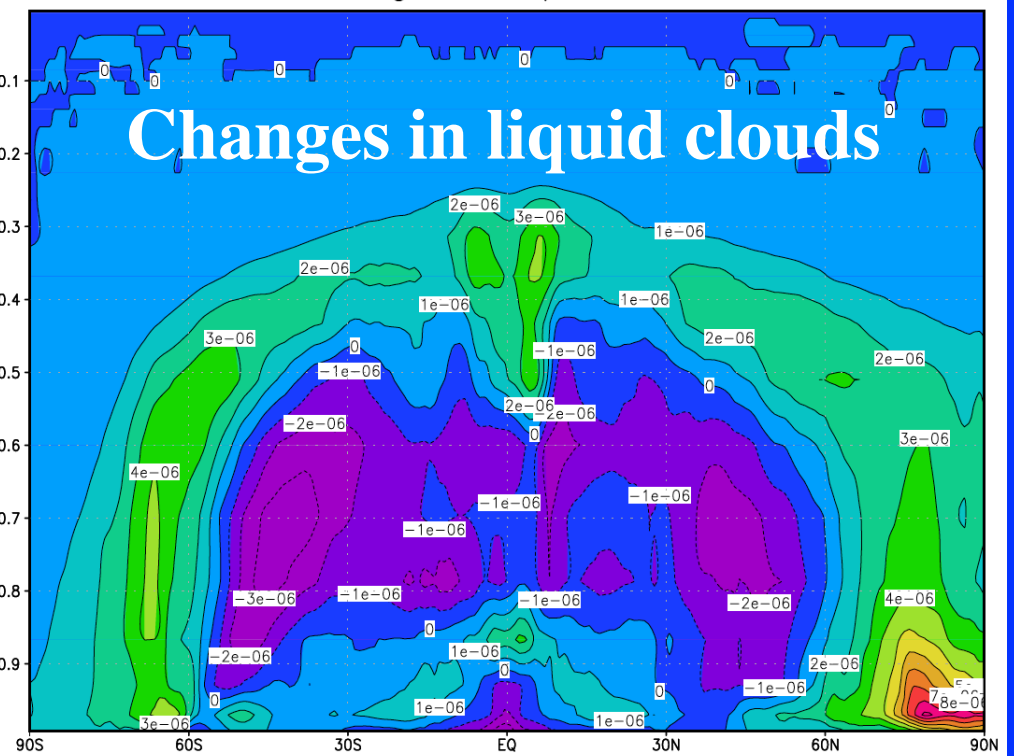
mean liquid clouds



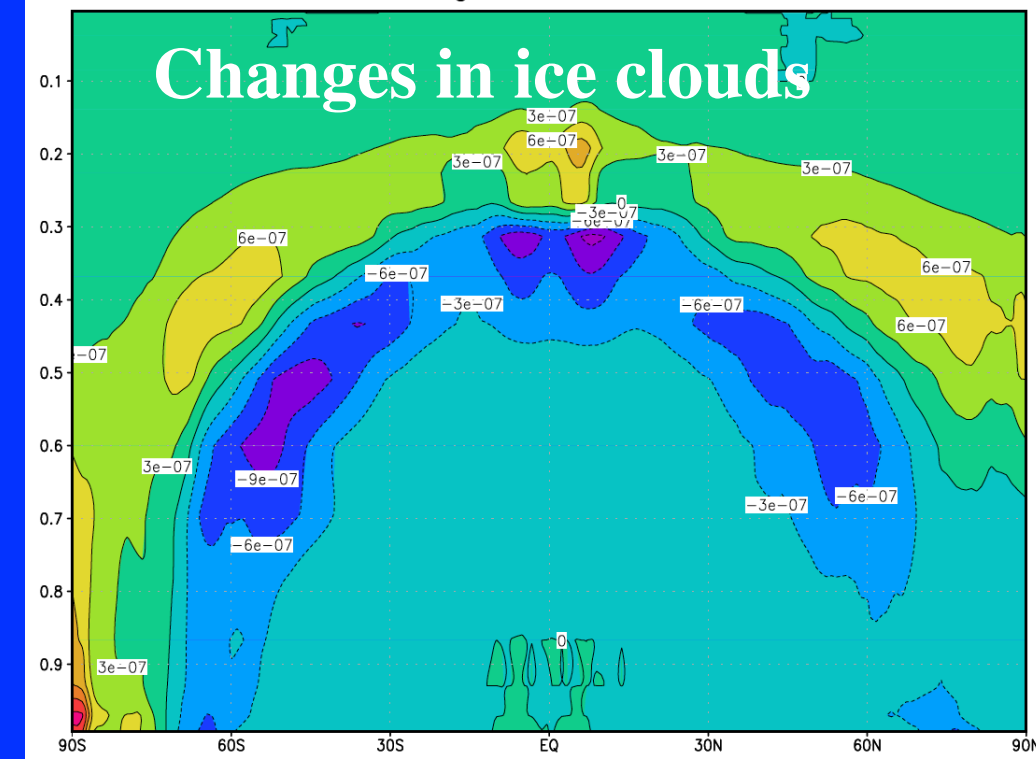
mean ice clouds



changes in liquid cloud

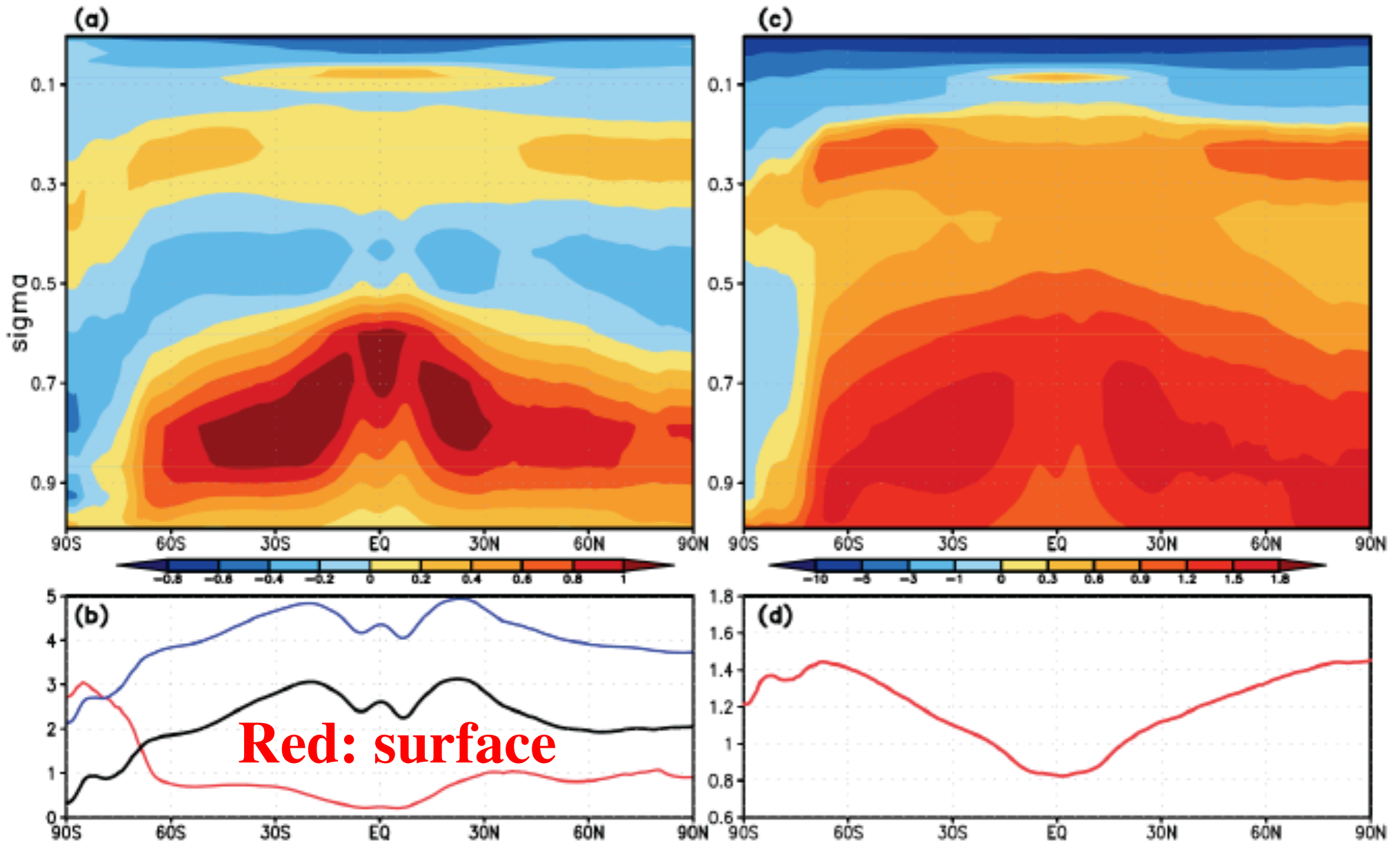


changes in ice cloud

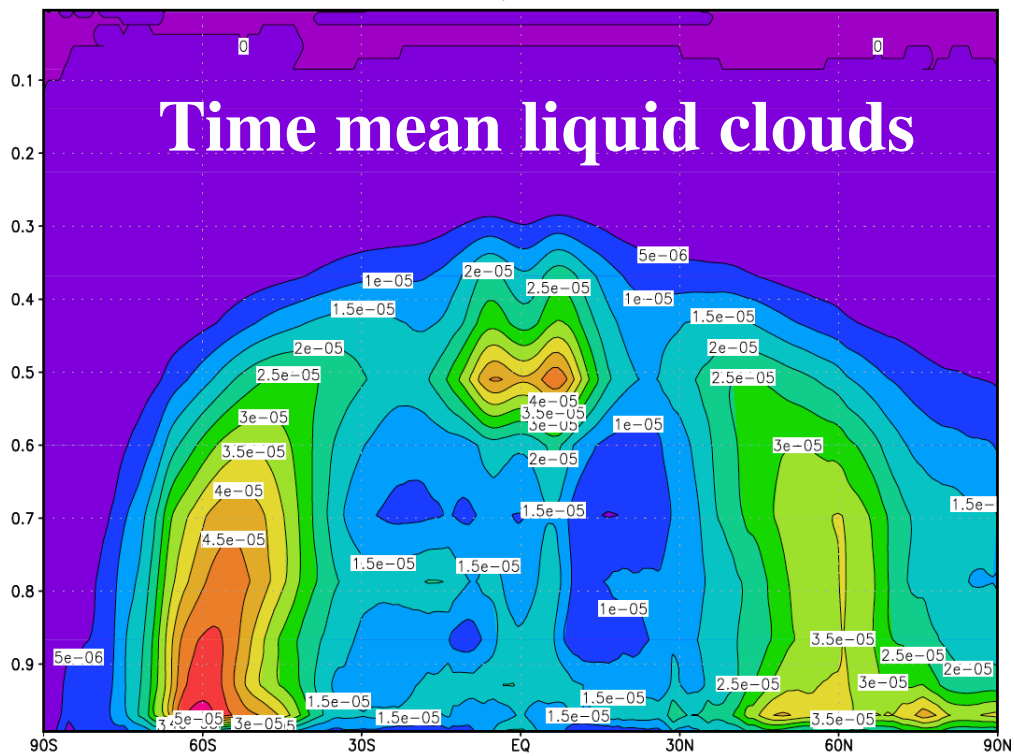


$$[\Delta F^{(EXT)}]$$

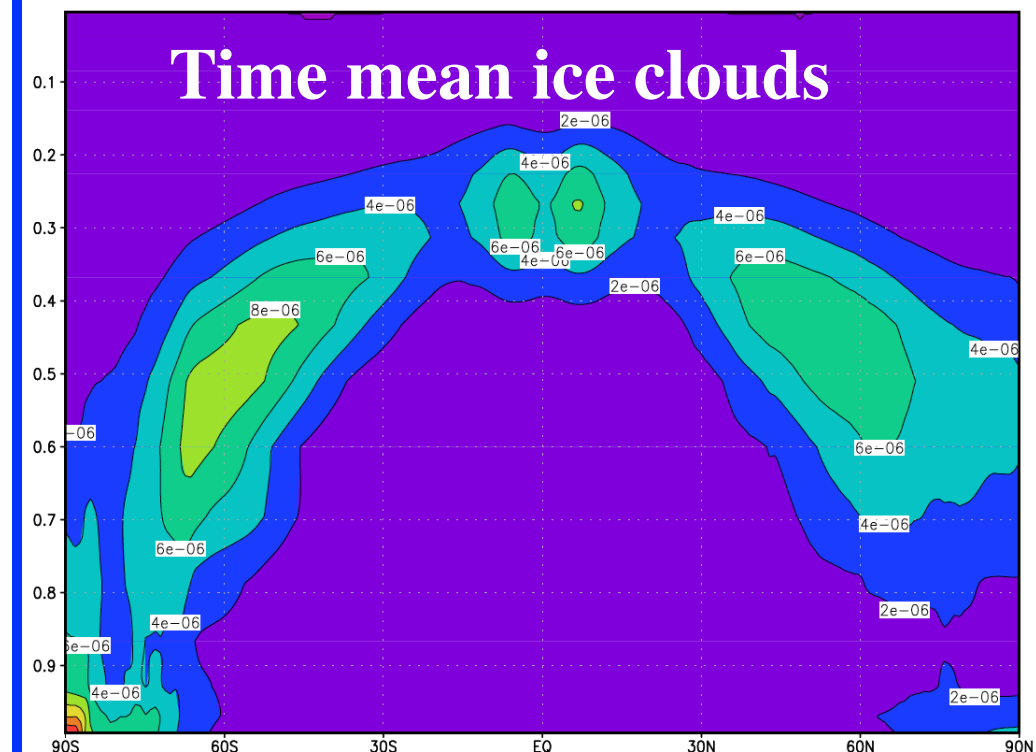
$$[\Delta T^{(EXT)}]$$



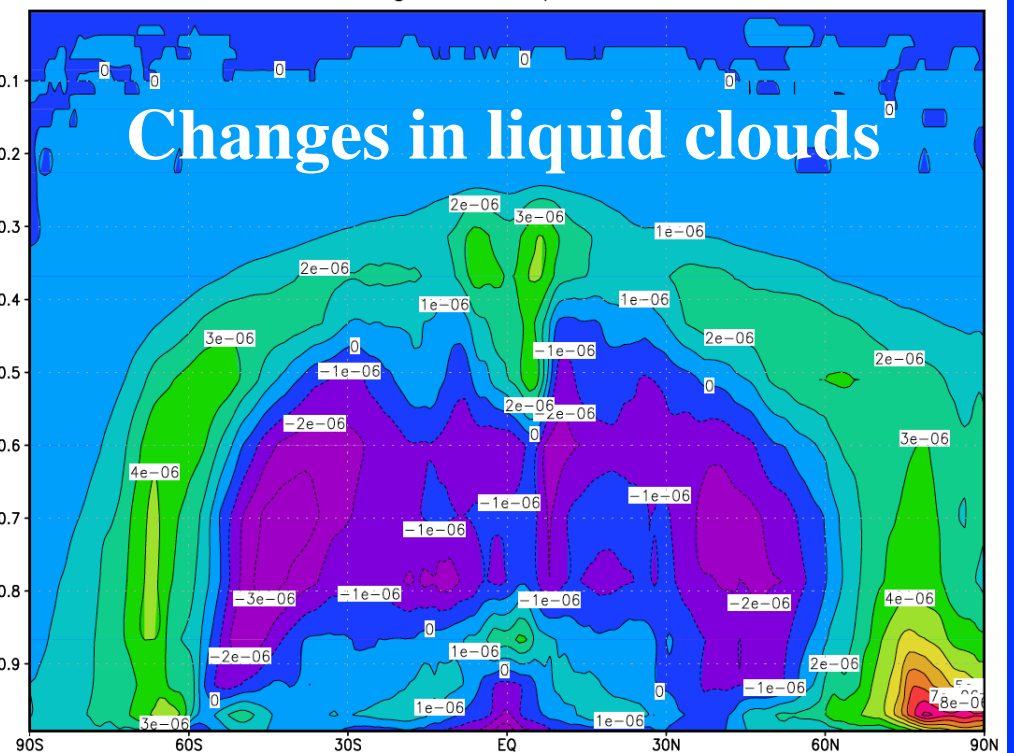
mean liquid clouds



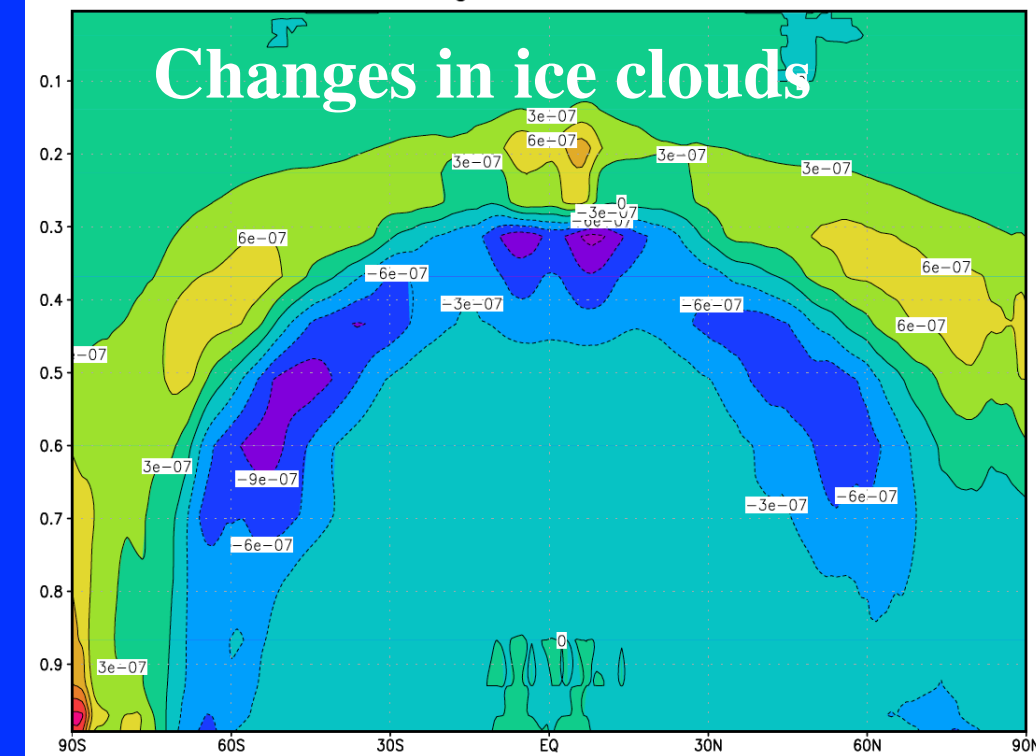
mean ice clouds



changes in liquid cloud



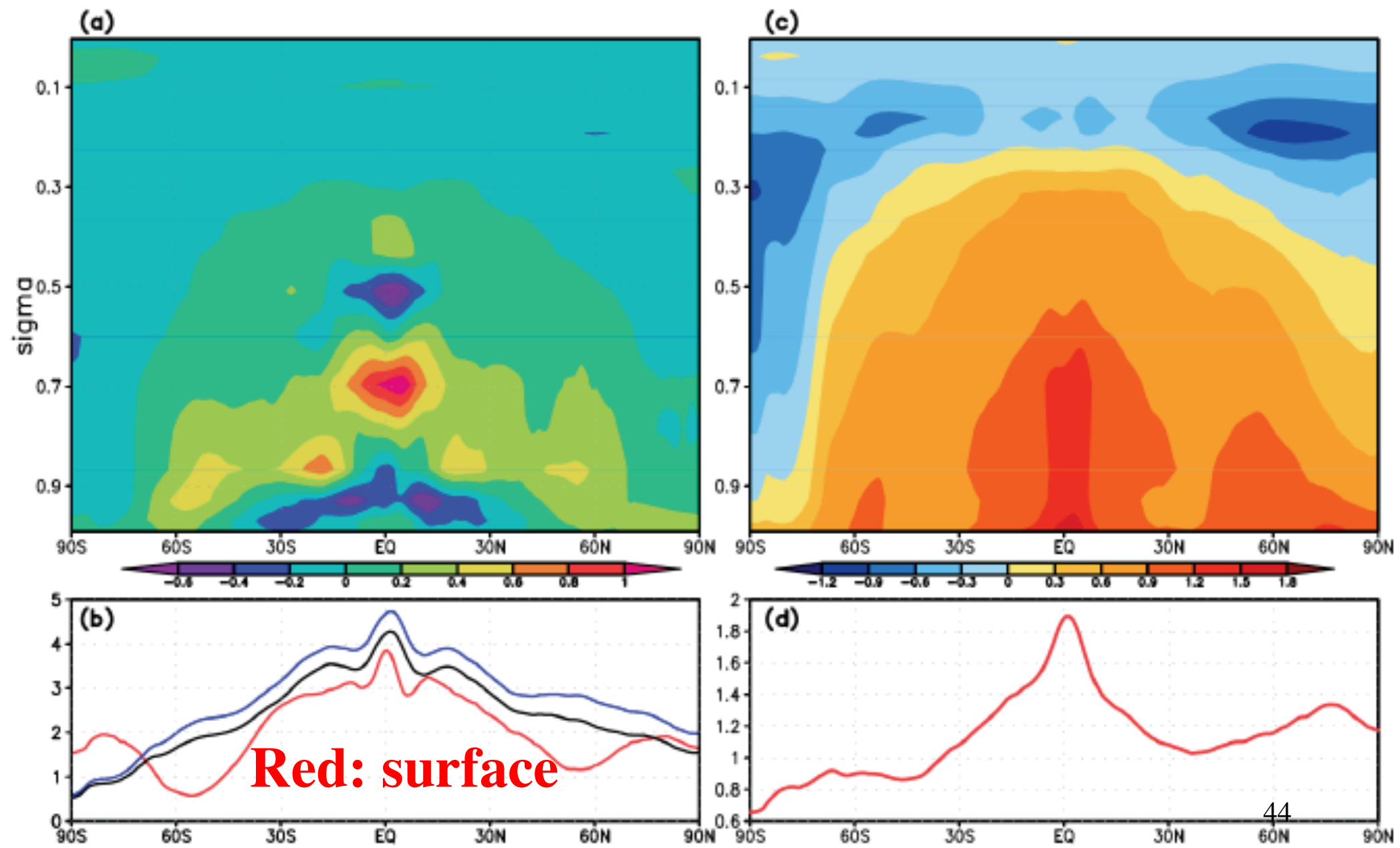
changes in ice cloud

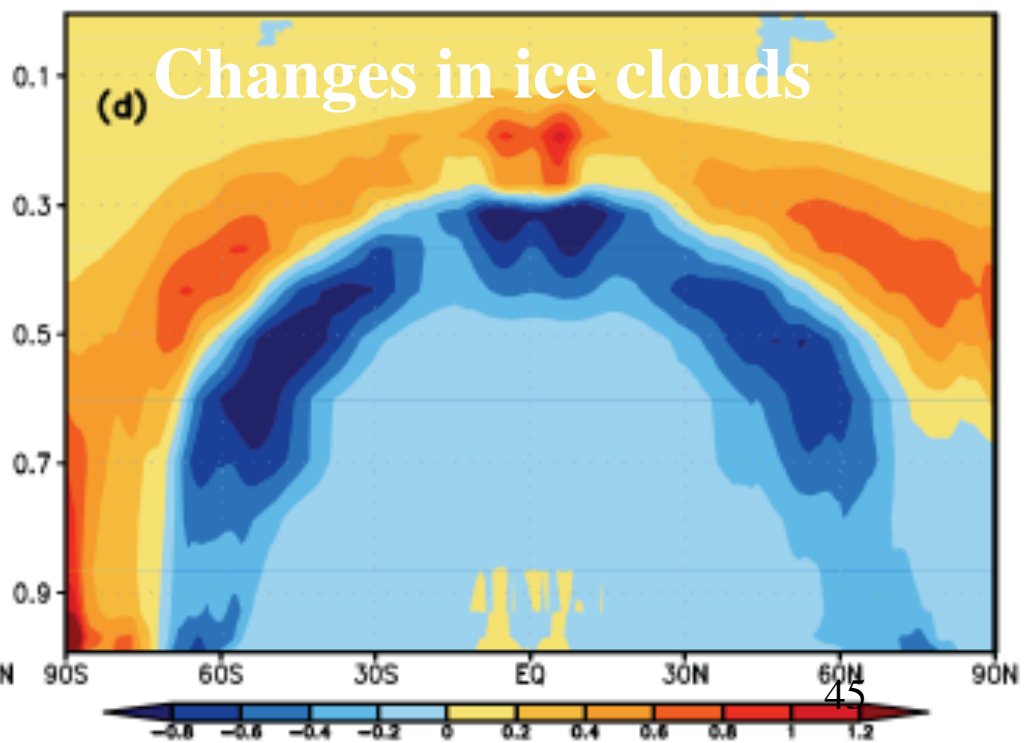
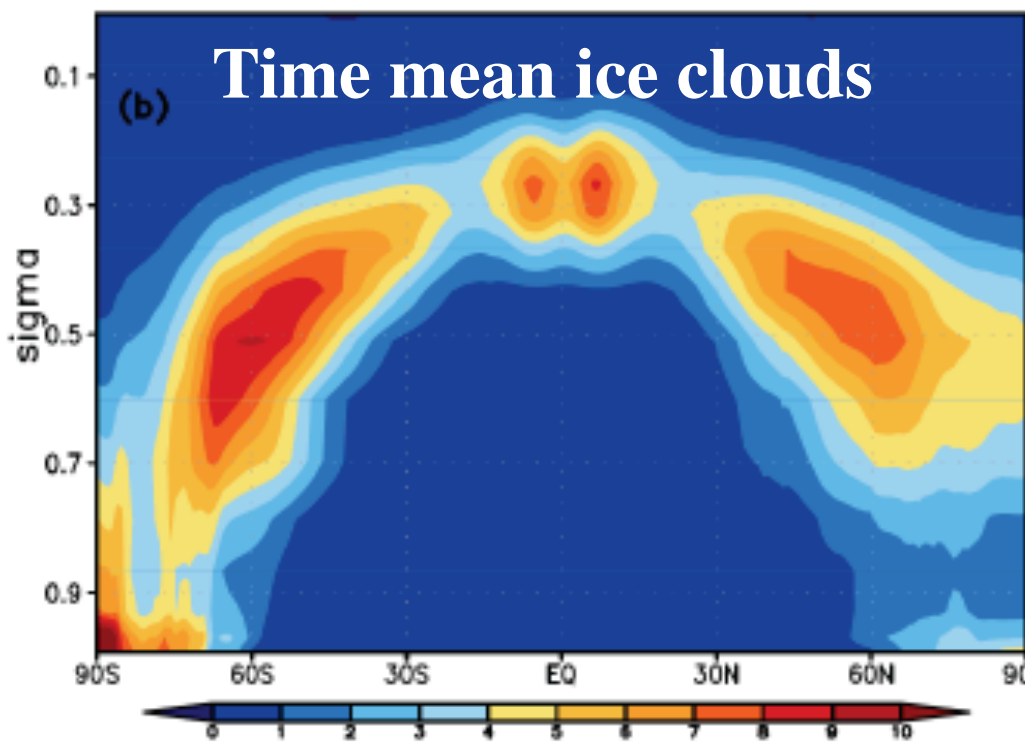
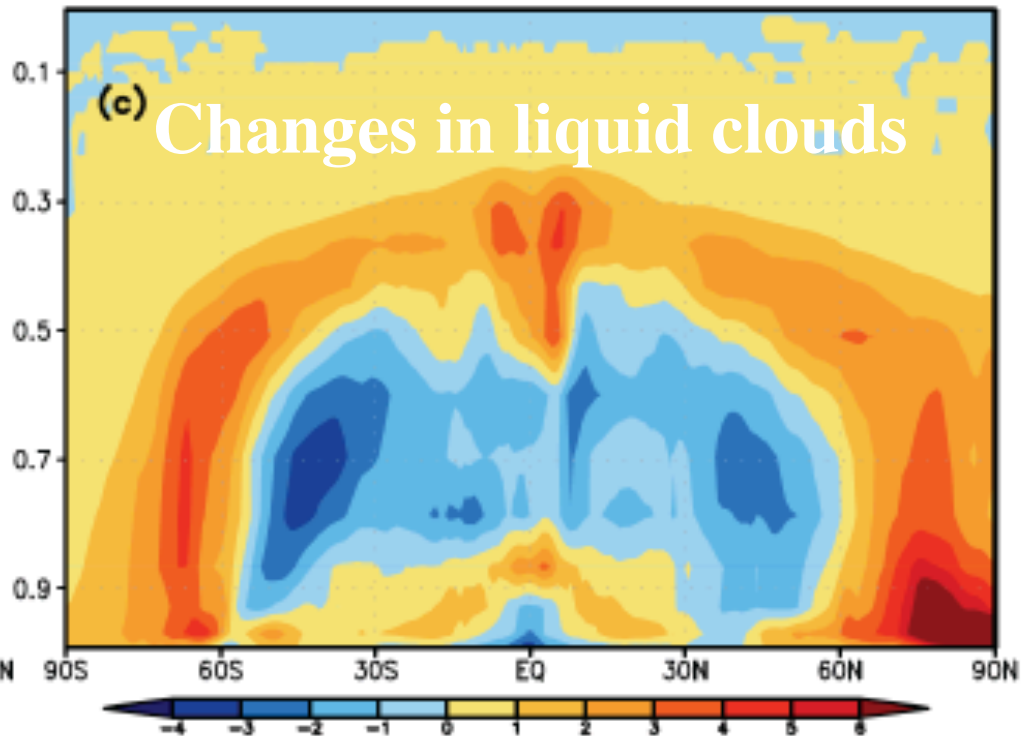
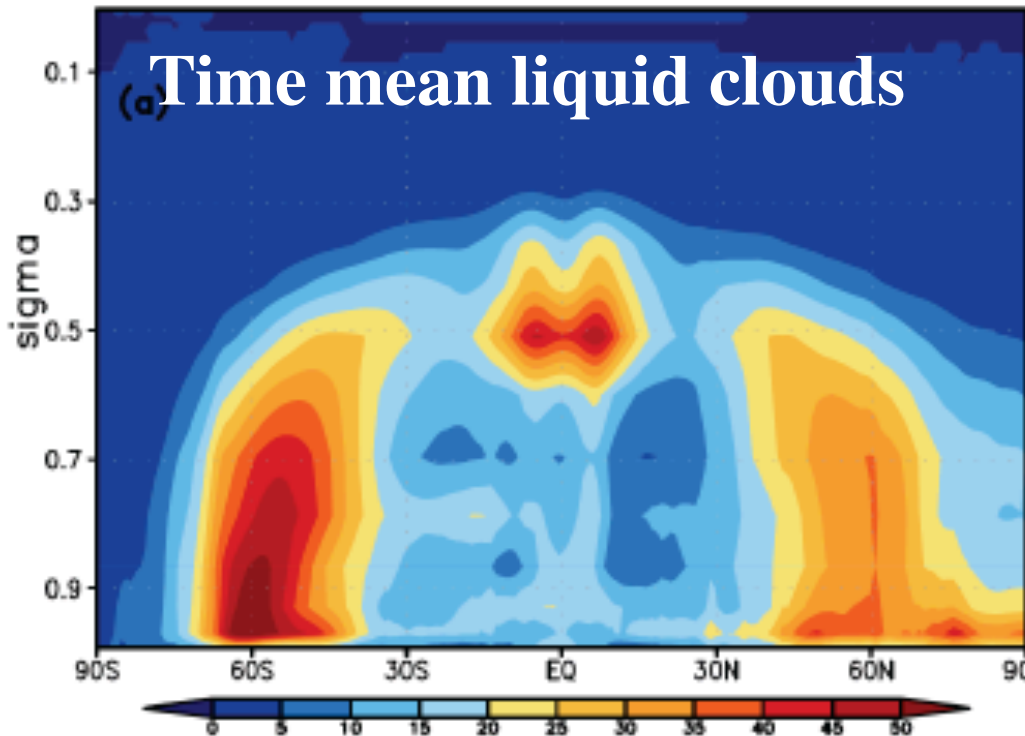




$$[\Delta F^{(WV)}]$$

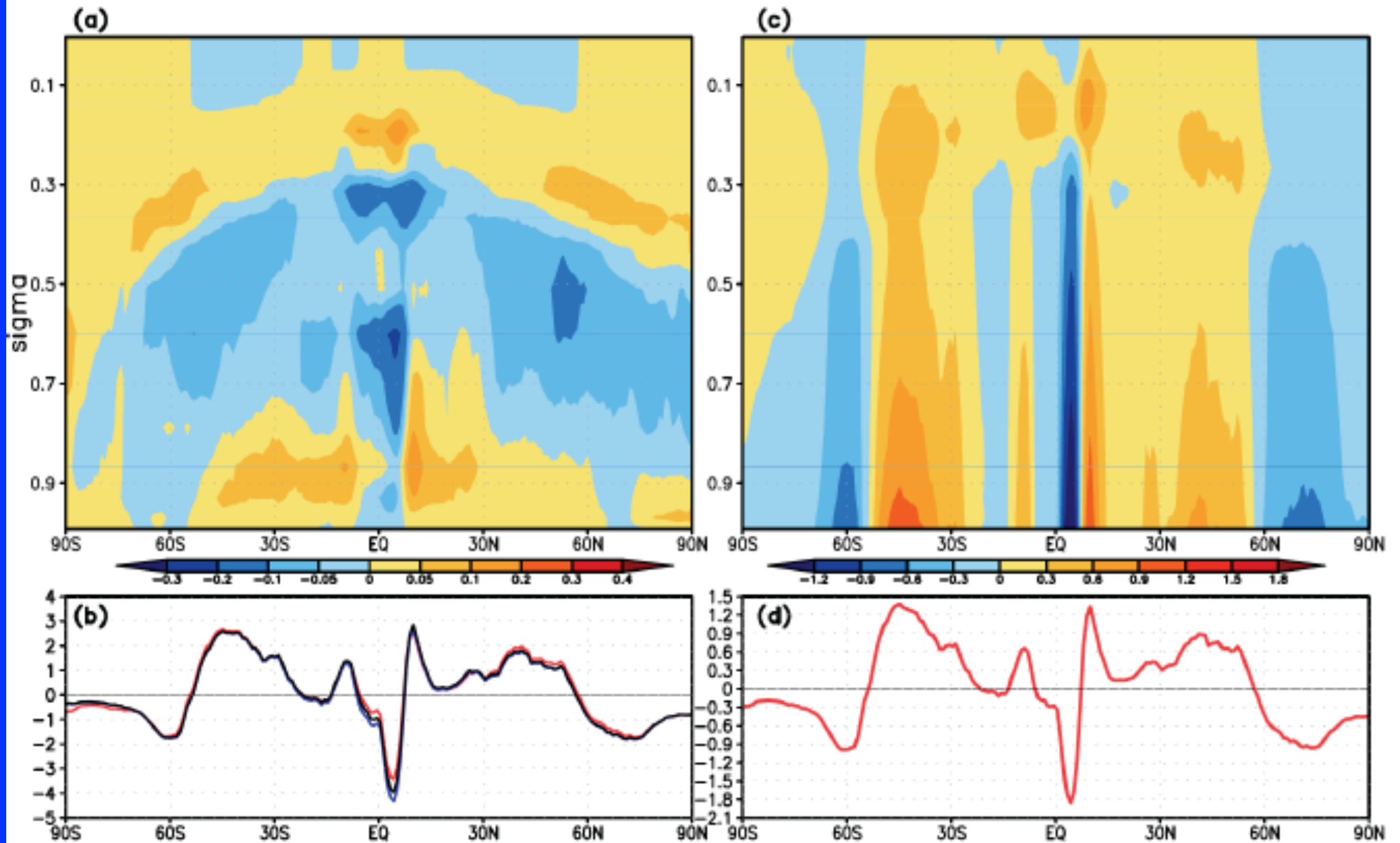
$$[\Delta T^{(WV)}]$$





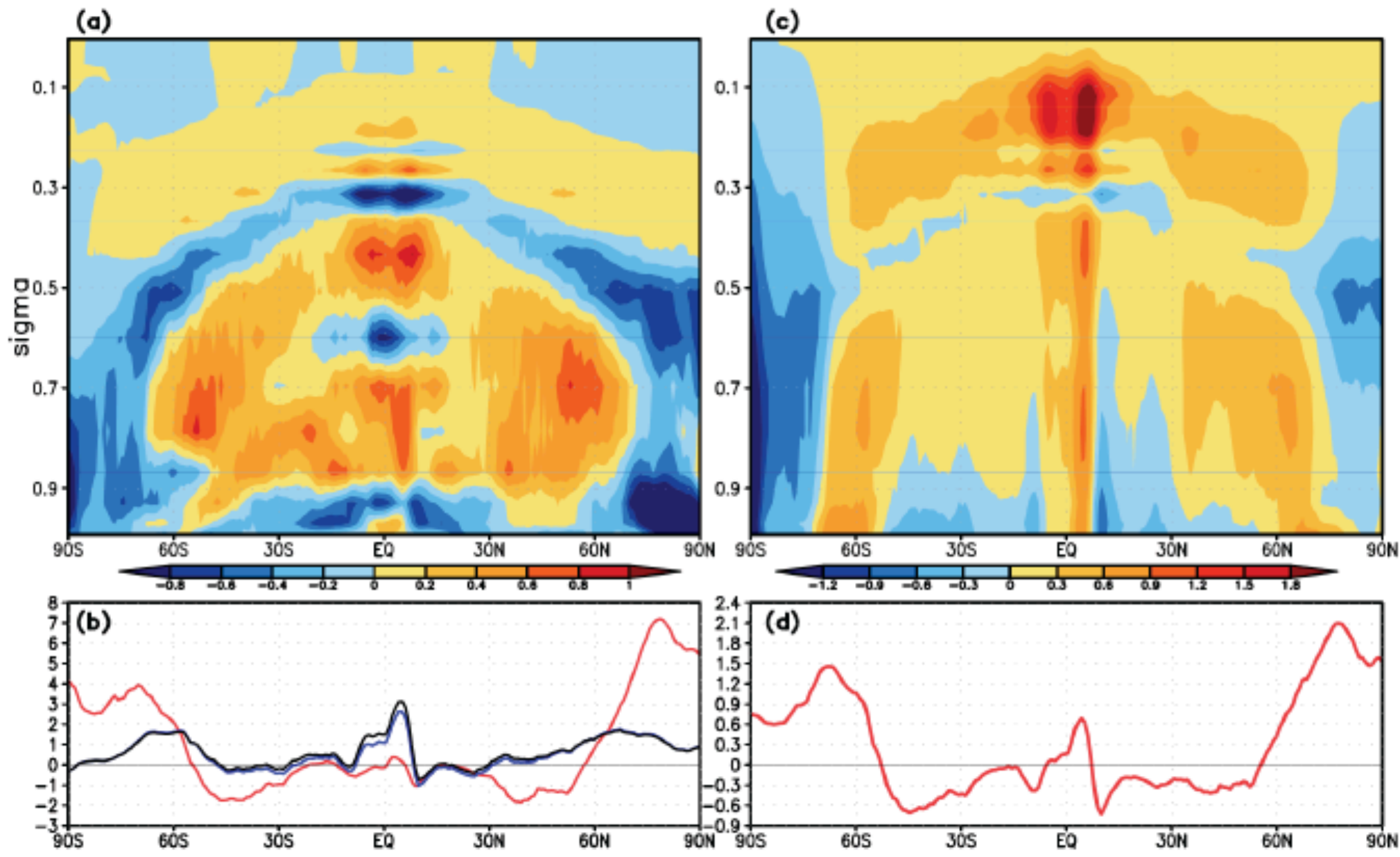
$$[\Delta F^{(Cloud\_SW)}]$$

$$[\Delta T^{(Cloud\_SW)}]$$



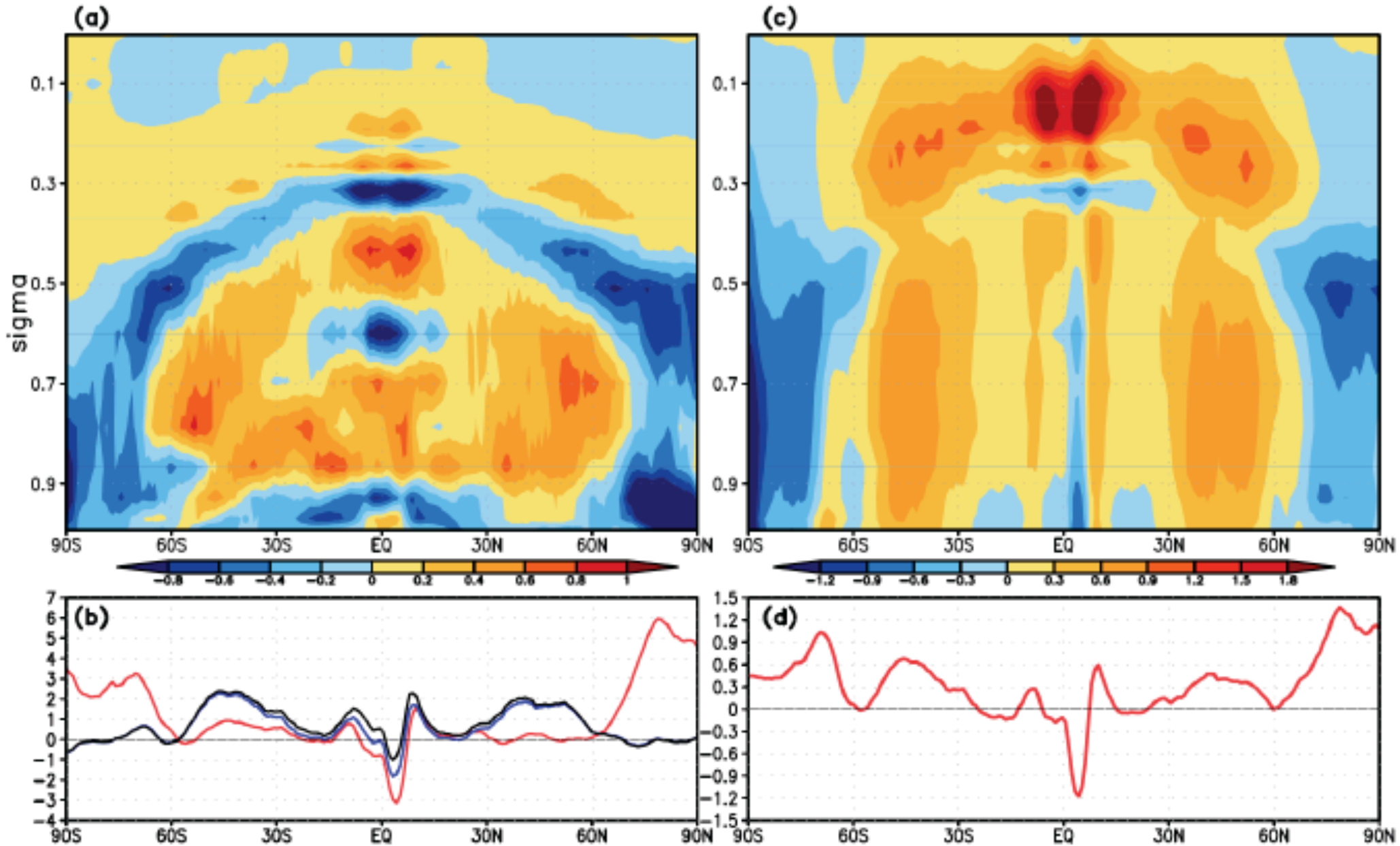
$$[\Delta F^{(Cloud\_LW)}]$$

$$[\Delta T^{(Cloud\_LW)}]$$



$$[\Delta F^{(Cloud\_NET)}]$$

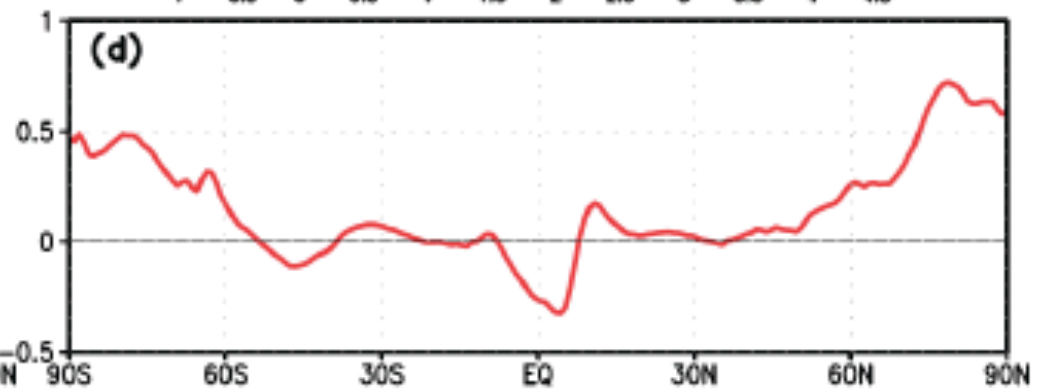
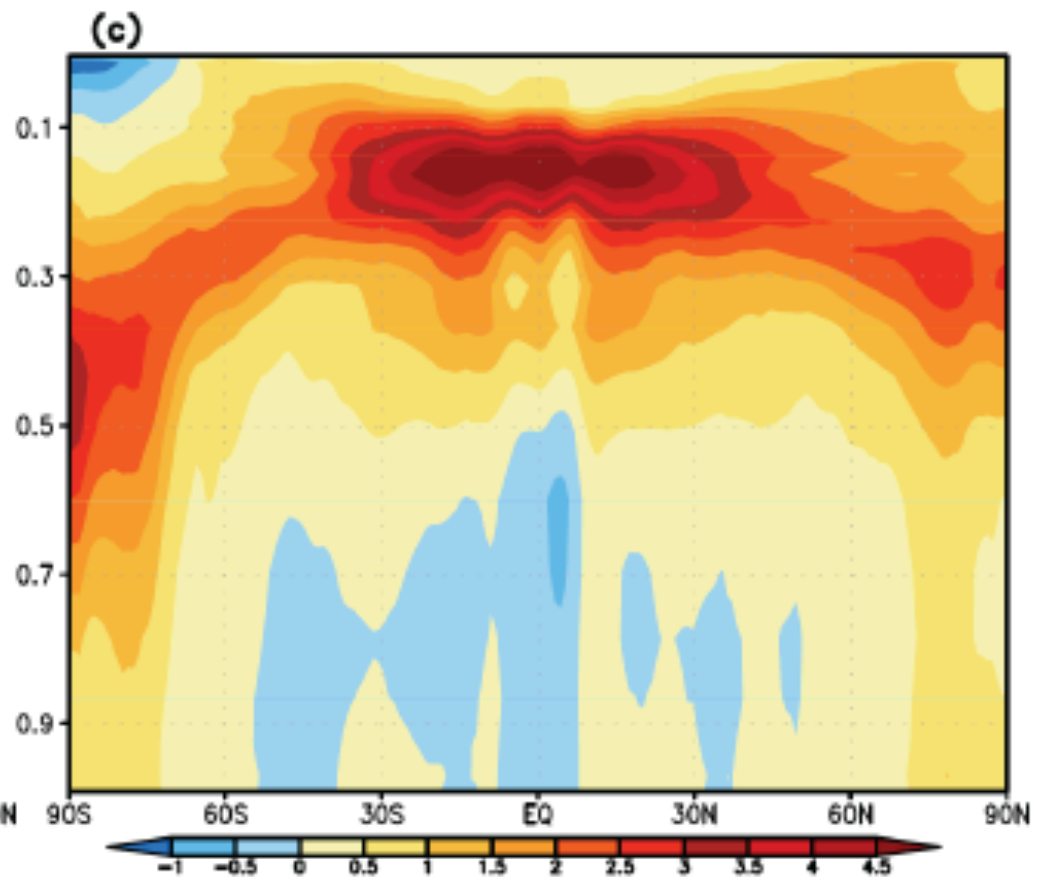
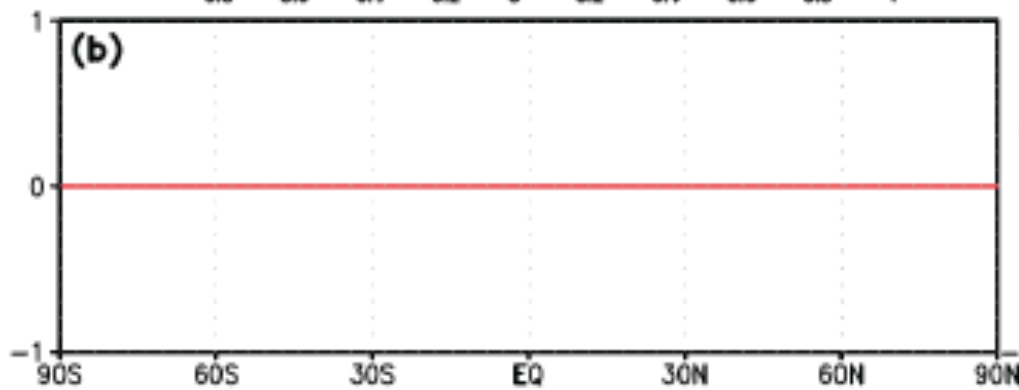
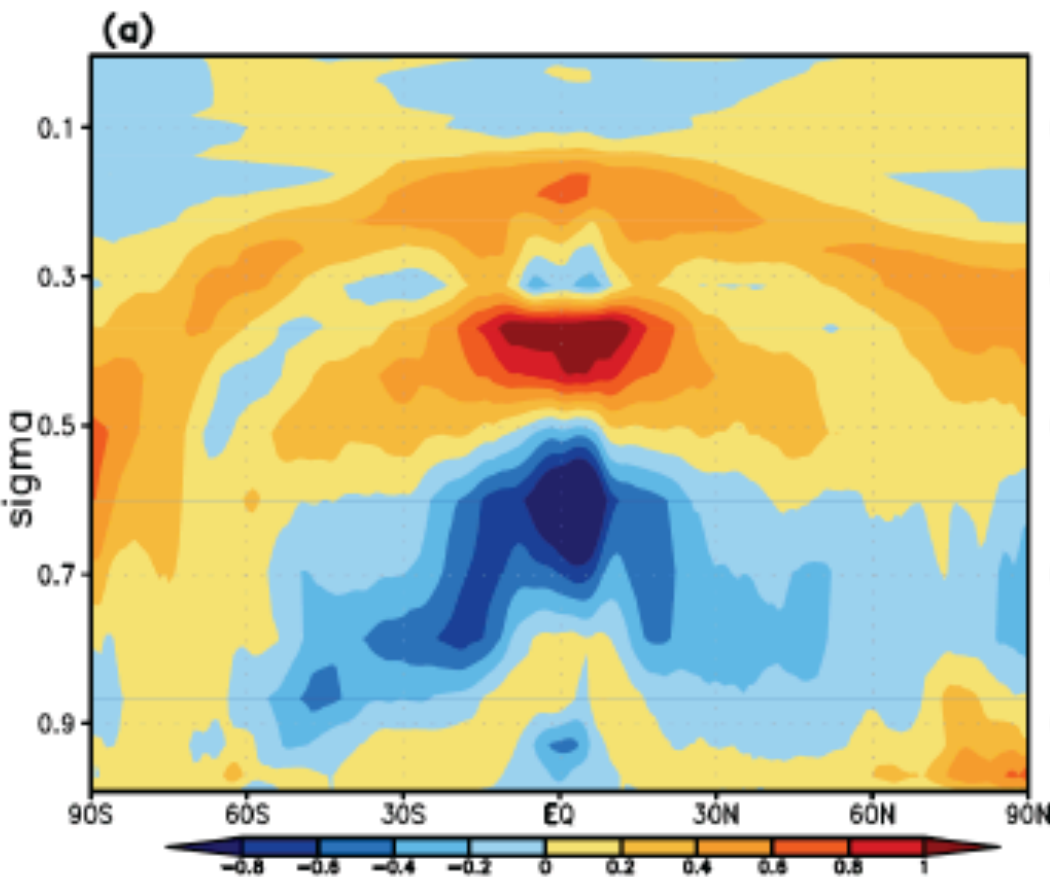
$$[\Delta T^{(Cloud\_NET)}]$$



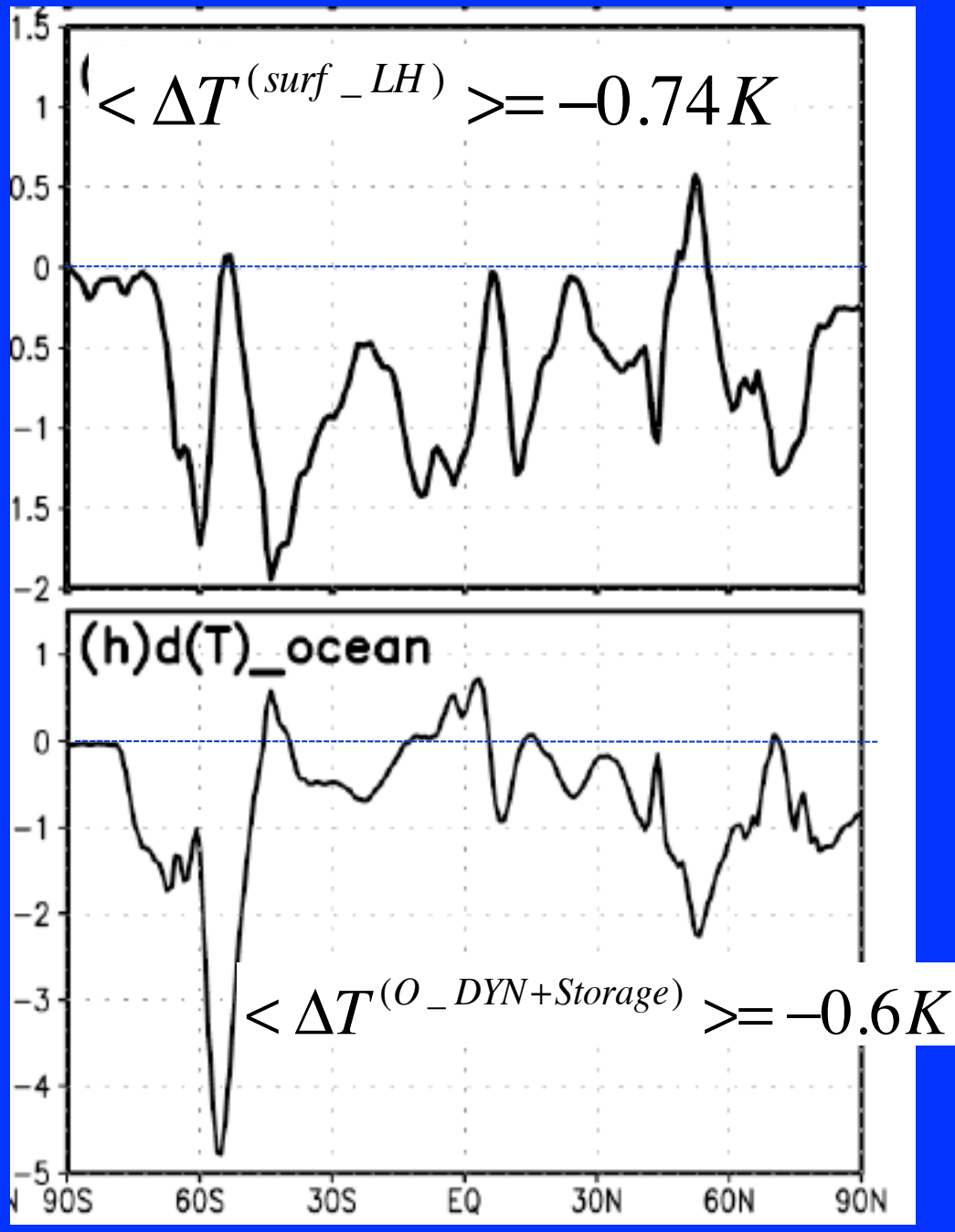
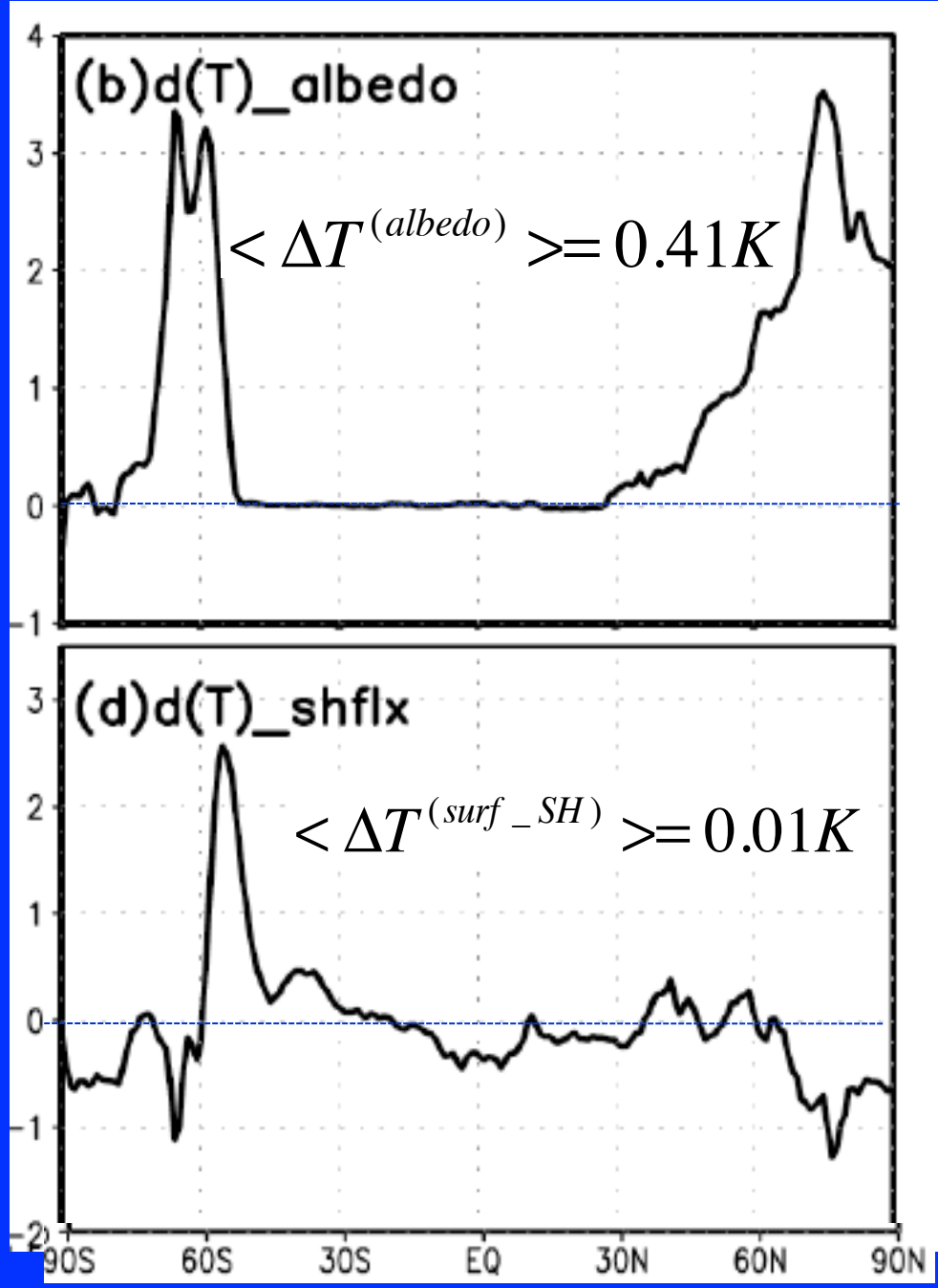


$$[\Delta F^{(Atmos\_DYN)}]$$

$$[\Delta T^{(Atmos\_DYN)}]$$

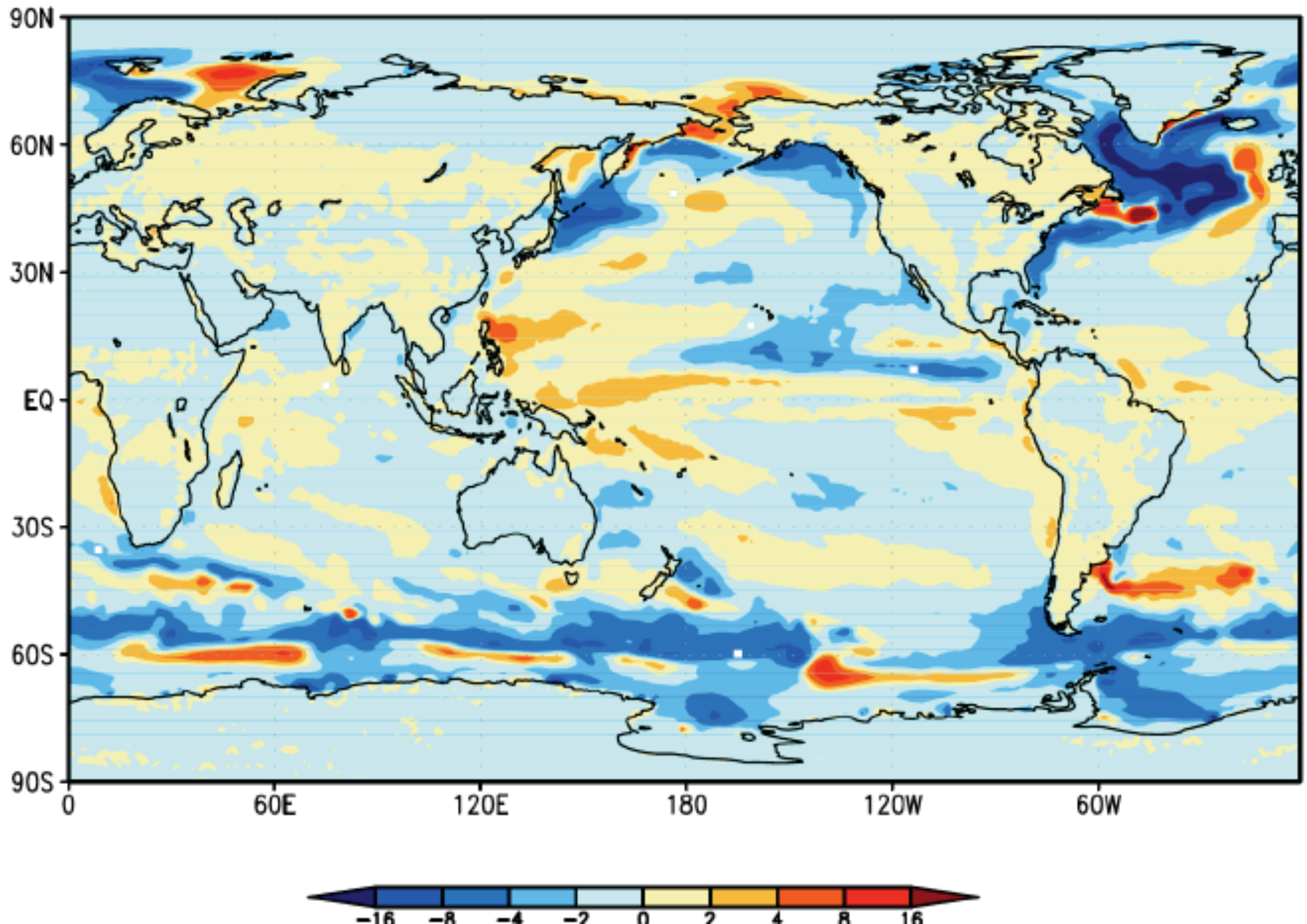




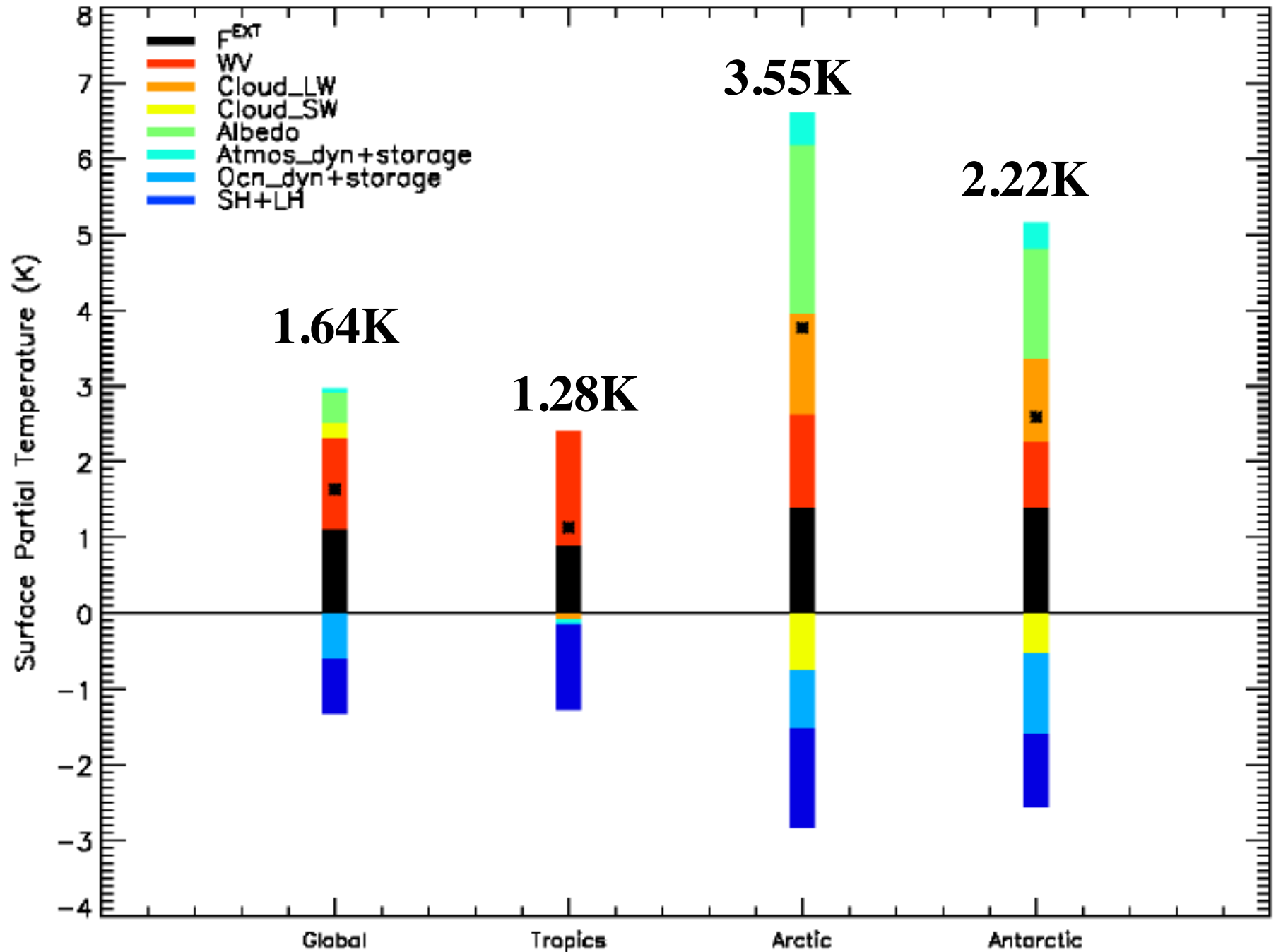


# Ocean transport and storage term

$$\langle \Delta T_{\text{ocean_dyn\_heat\_storage}} \rangle = -0.60\text{K}$$



# Attributions



# Summary 2

- **The linearization of radiation transfer model is a good approximation for global warming climate feedback analysis.**
- **Sum of partial temp. changes is very close to the total temp. change (validation of CFRAM).**
- **2CO<sub>2</sub> forcing and water vapor feedback tend to create largest warming at the lower troposphere and surface.**
- **Evaporation feedback acts to reduce warming over the vast global surface while cloud shortwave radiative feedback mainly reduces warming over the warm pool area.**
- **Cloud longwave radiative and atmospheric dynamical (non-radiative) feedbacks tend to place larger warming in upper troposphere.**
- **2CO<sub>2</sub> forcing, cloud longwave, and surface albedo radiative feedbacks and atmospheric dynamical feedbacks all contribute to stronger surface warming at high latitudes.**
- **Atmospheric circulation expands upward and poleward.**